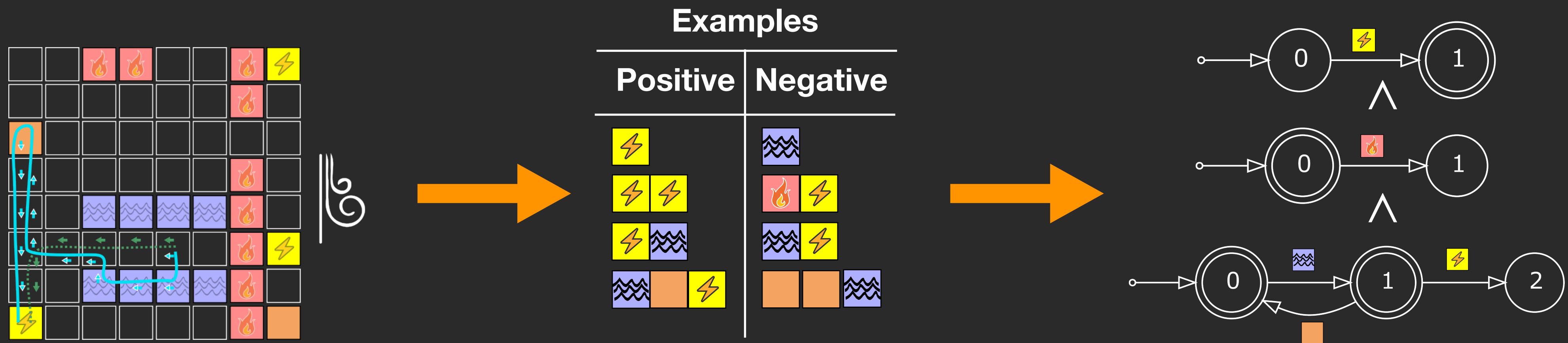


# Learning DFA Decompositions from Examples and Demonstrations

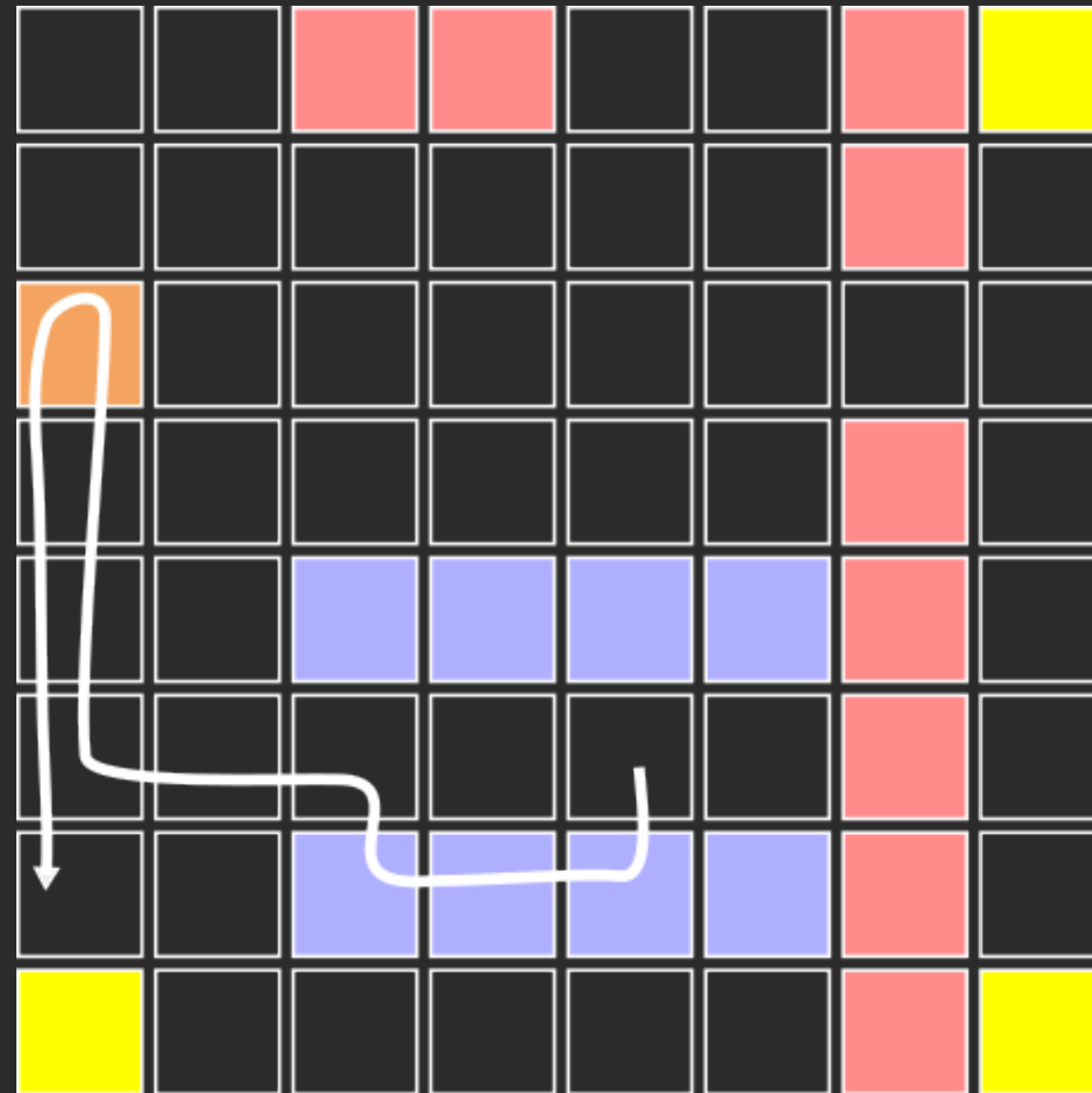


Niklas Lauffer<sup>\*</sup>, Beyazit Yalcinkaya<sup>\*</sup>, Marcell Vazquez-Chanlatte, Ameesh Shah, and Sanjit A. Seshia

<sup>\*</sup>equal contribution

University of California, Berkeley

# A simple gridworld

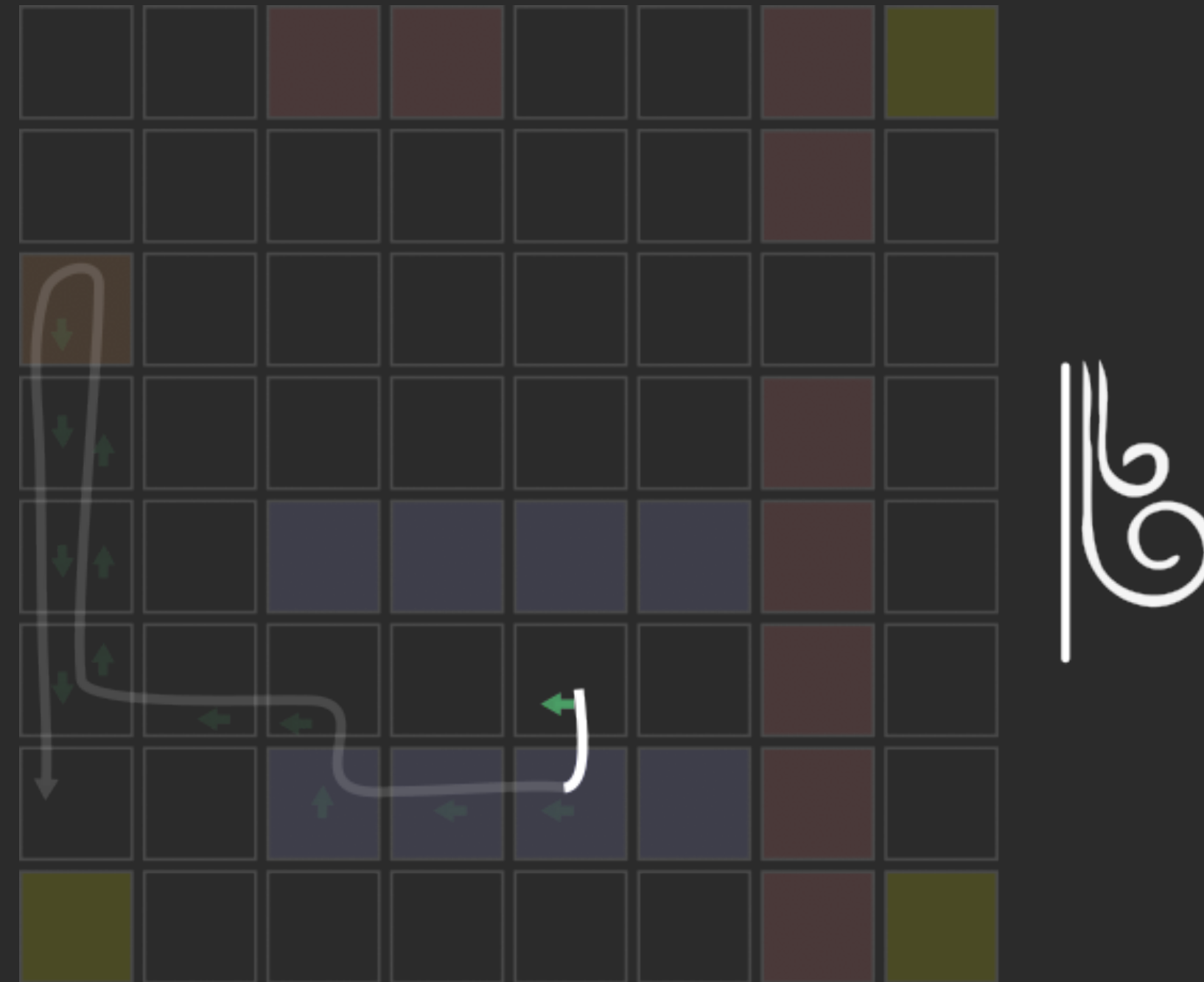


# A simple gridworld



Actions = {   

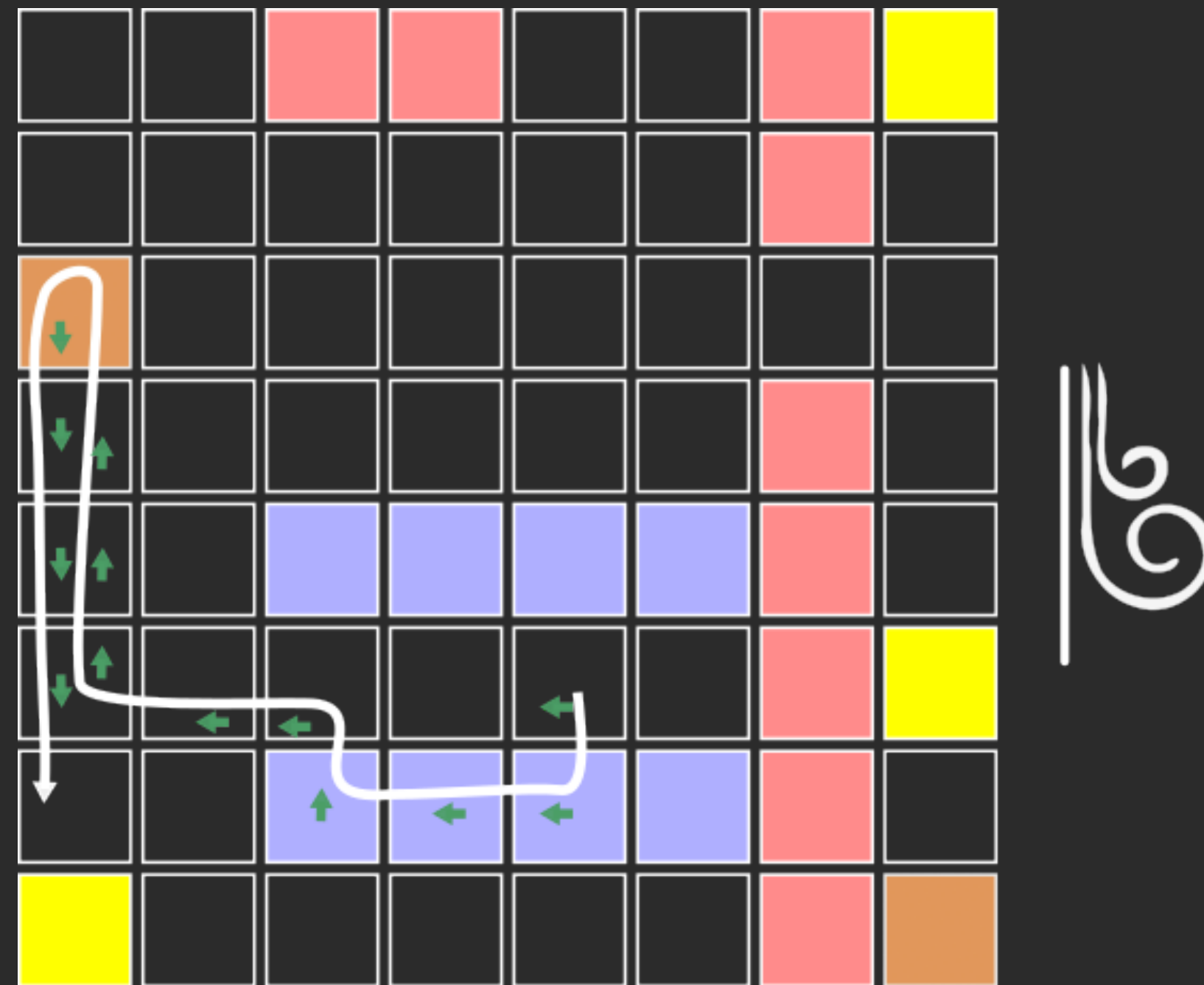
# A simple gridworld



Actions = {   

$\Pr(\text{slip } \downarrow) = 1/32$

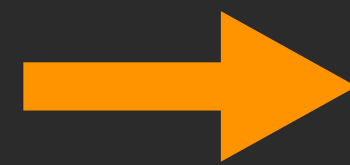
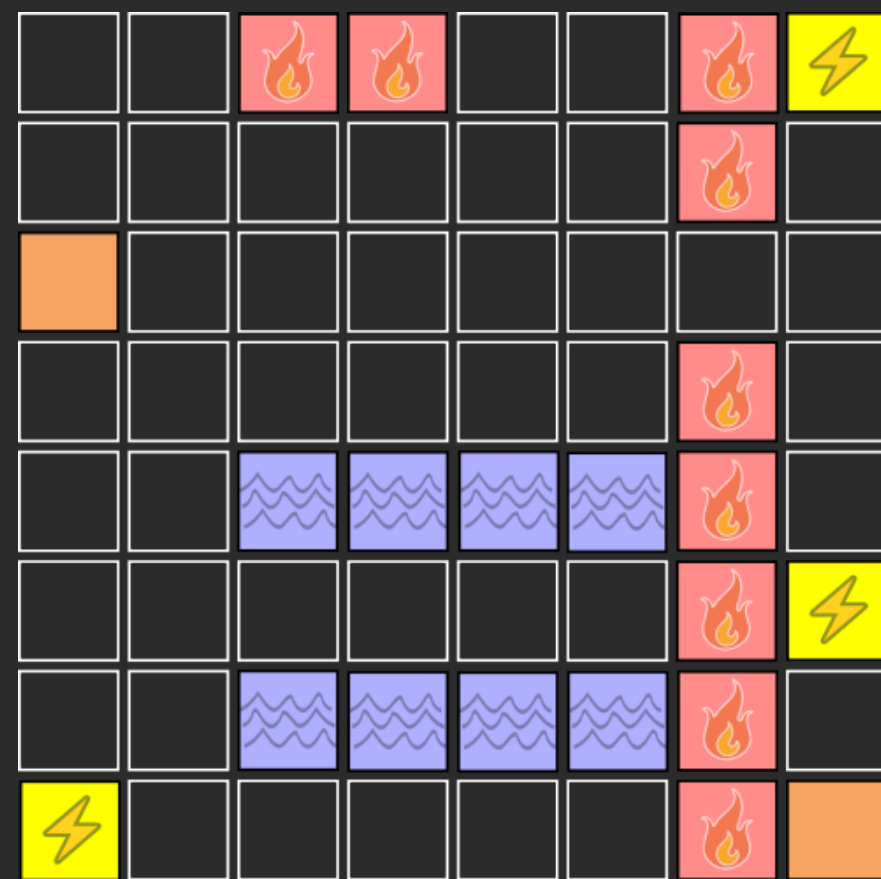
# A simple gridworld



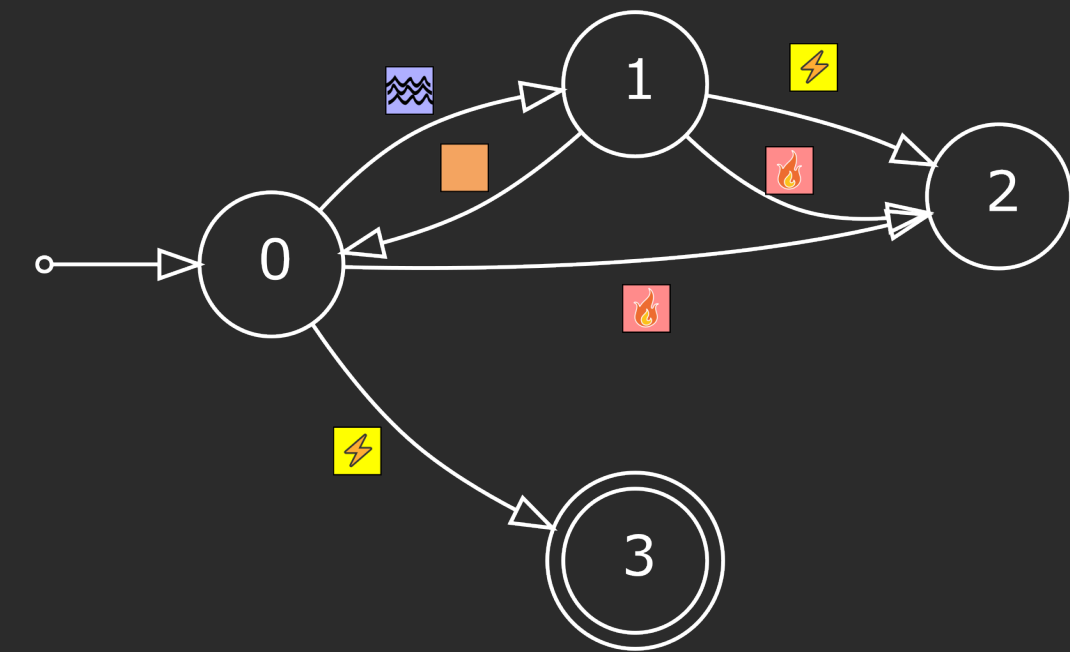
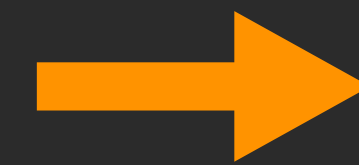
Actions = { $\uparrow$   $\downarrow$   $\leftarrow$   $\rightarrow$ }

$\Pr(\text{slip } \downarrow) = 1/32$

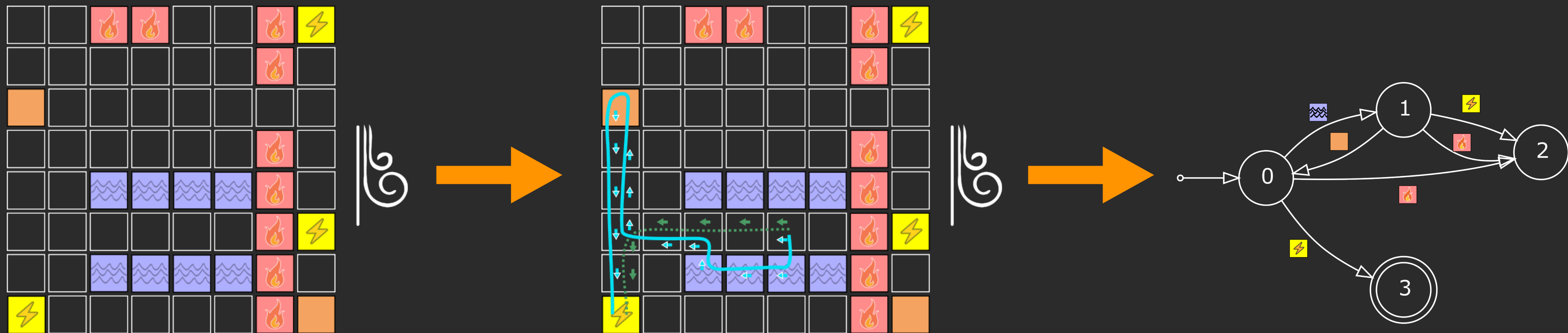
# Specification mining



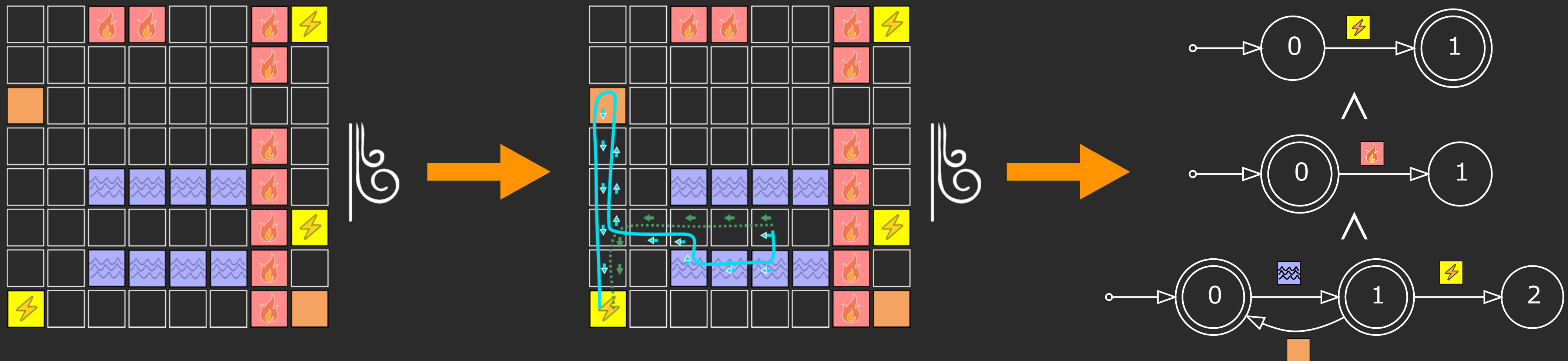
Examples	
Positive	Negative
⚡	🌊
⚡ ⚡	🔥 ⚡
⚡ 🌊	🌊 ⚡
🌊 🟠 ⚡	🟠 🟠 🌊



# Learning from demonstrations



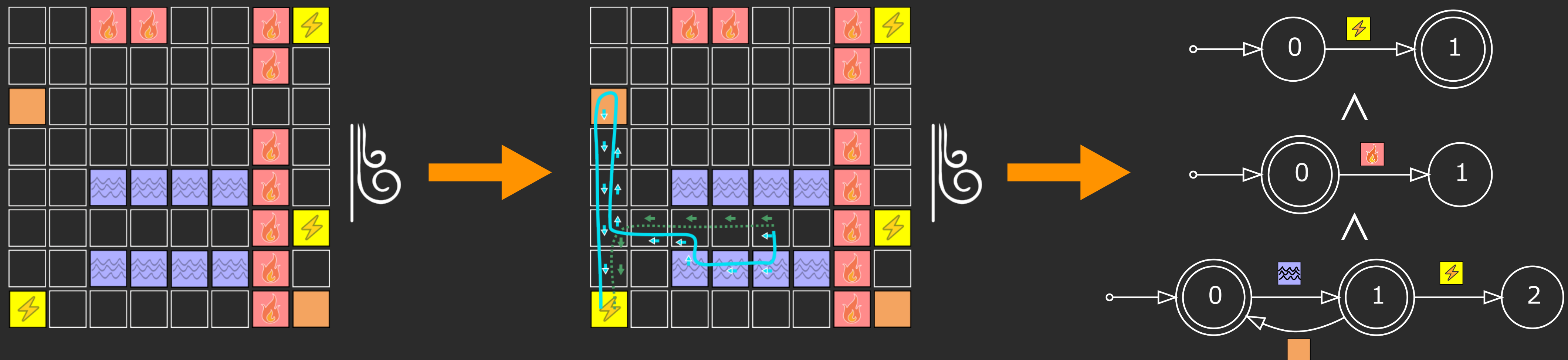
# Learning decompositions



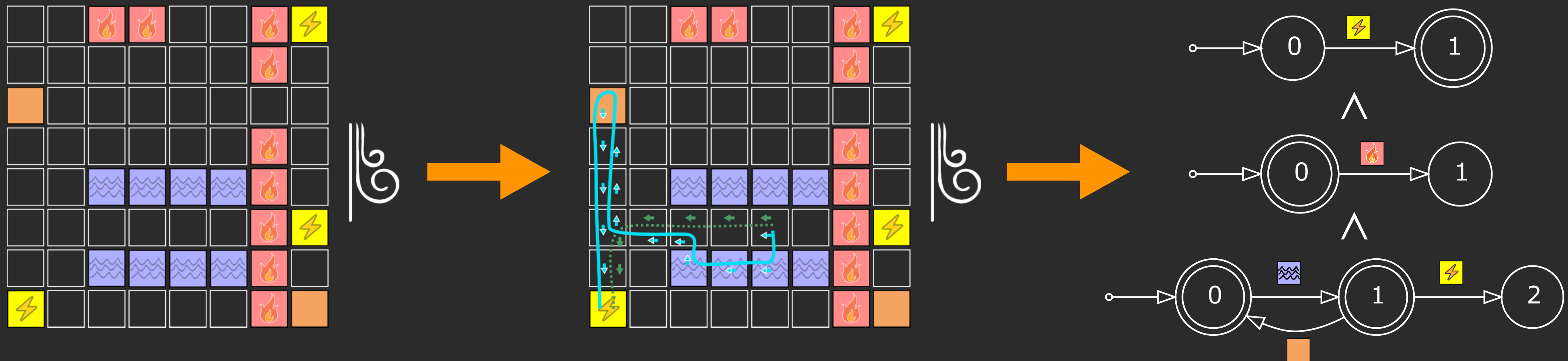




# System-level specifications are often conjunctions of sub-specifications



# Inductive bias matters when learning from few demonstrations



# Contributions

1. SAT-based encoding for identifying a DFA decomposition of a specific size from labeled examples

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2. An algorithm for enumerating the full Pareto-frontier of decompositions

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1. SAT-based encoding for identifying a DFA decomposition of a specific size from labeled examples
2. An algorithm for enumerating the full Pareto-frontier of decompositions
3. Experimental analysis and extension to learning from demonstrations

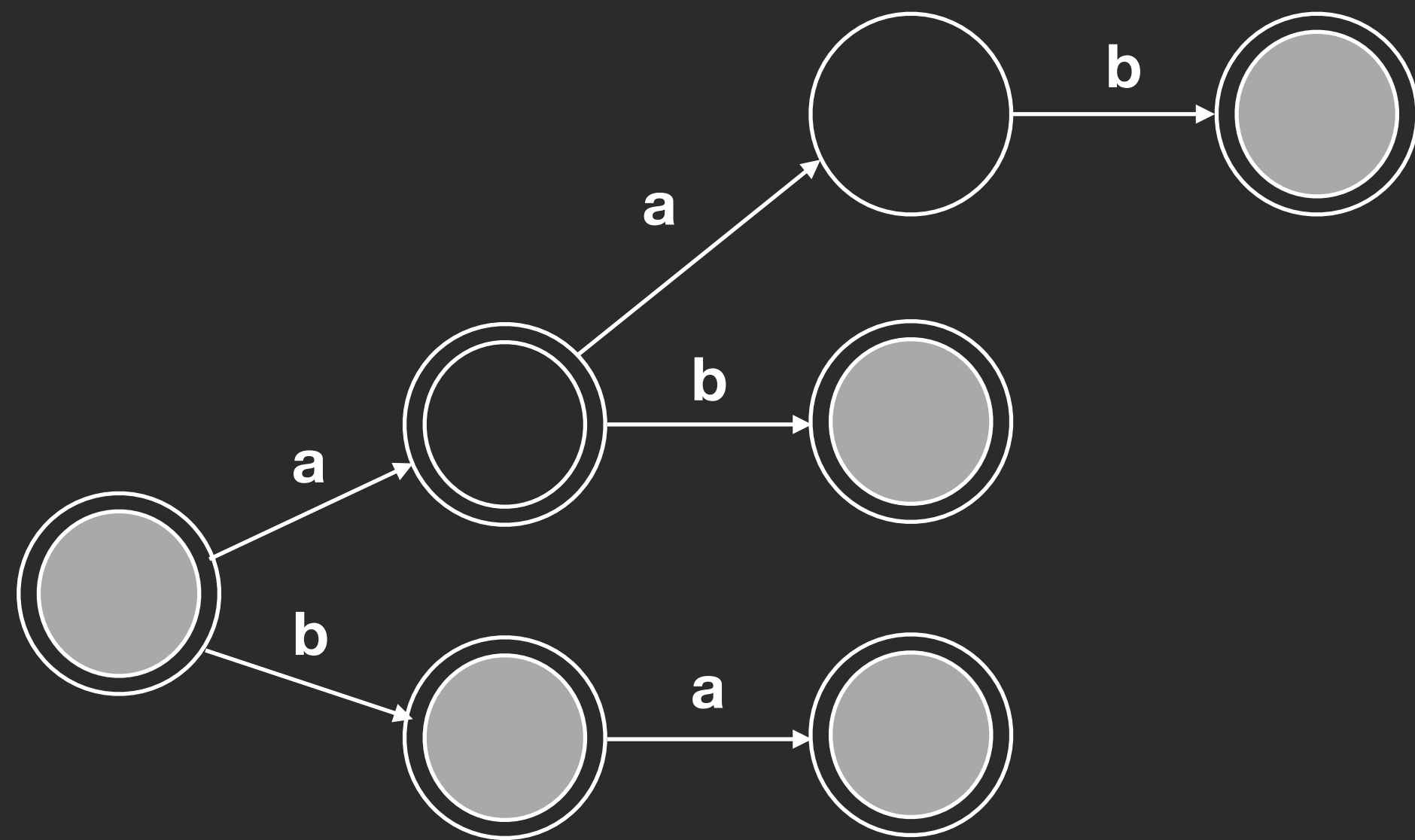
# Structure of the talk

1. Technical details

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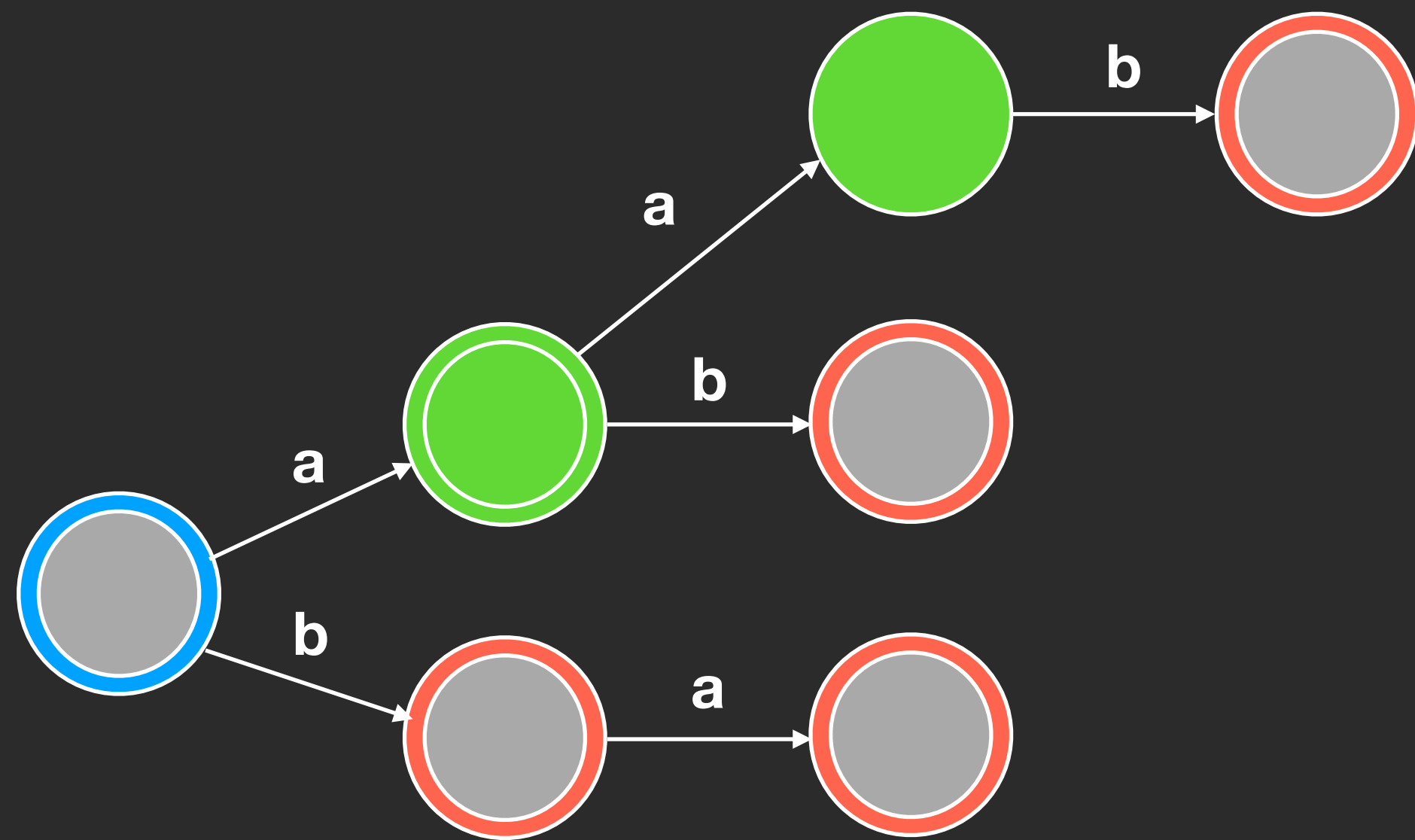
# State merging via coloring



Positive: {a}    Negative: { $\emptyset$ , b, ba, ab, aab}



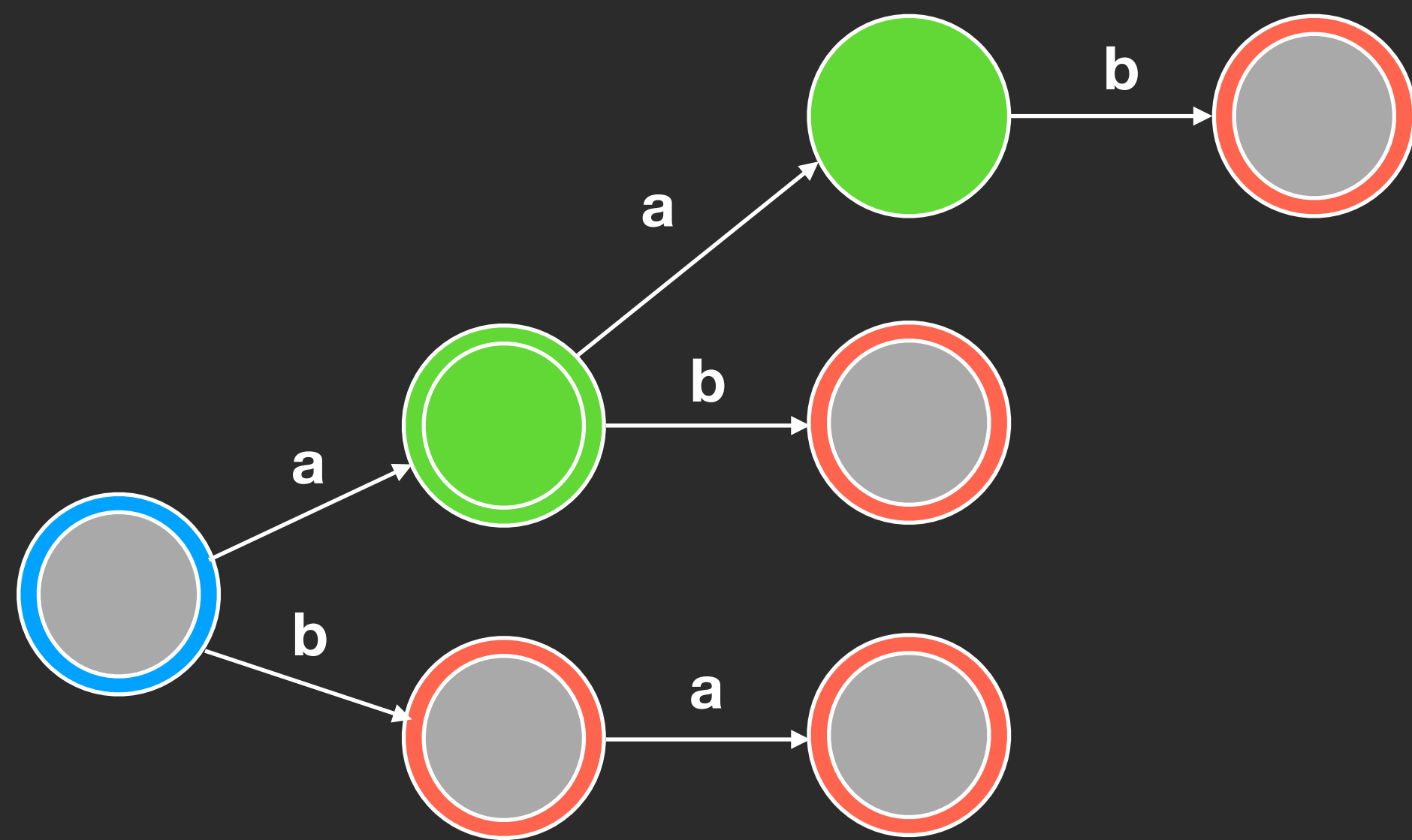
# State merging via coloring



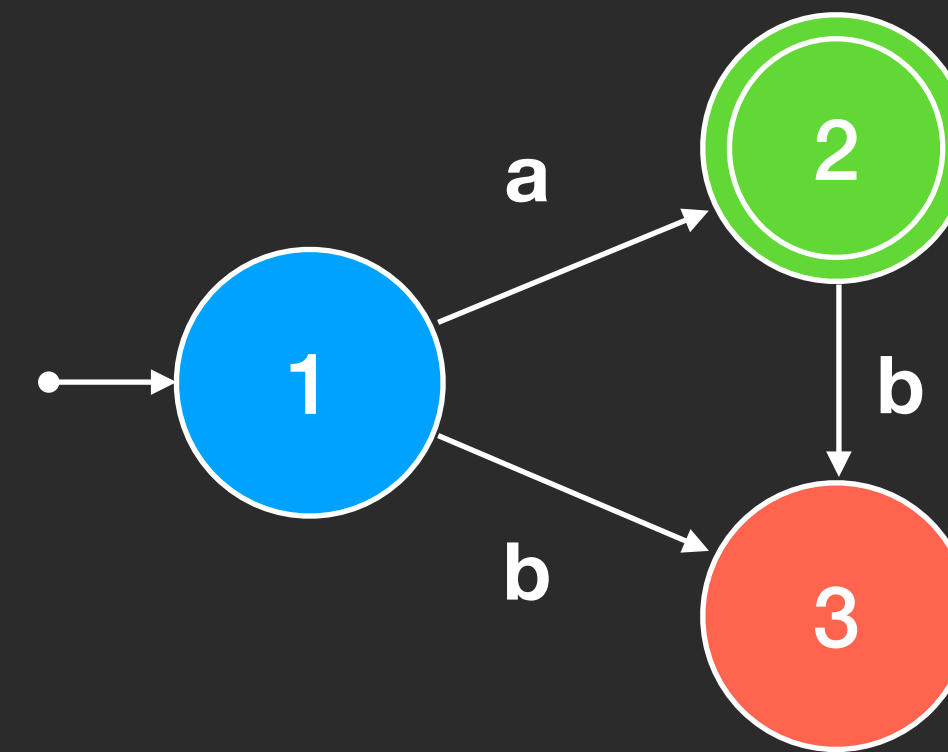
Positive: {a}

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# State merging via coloring

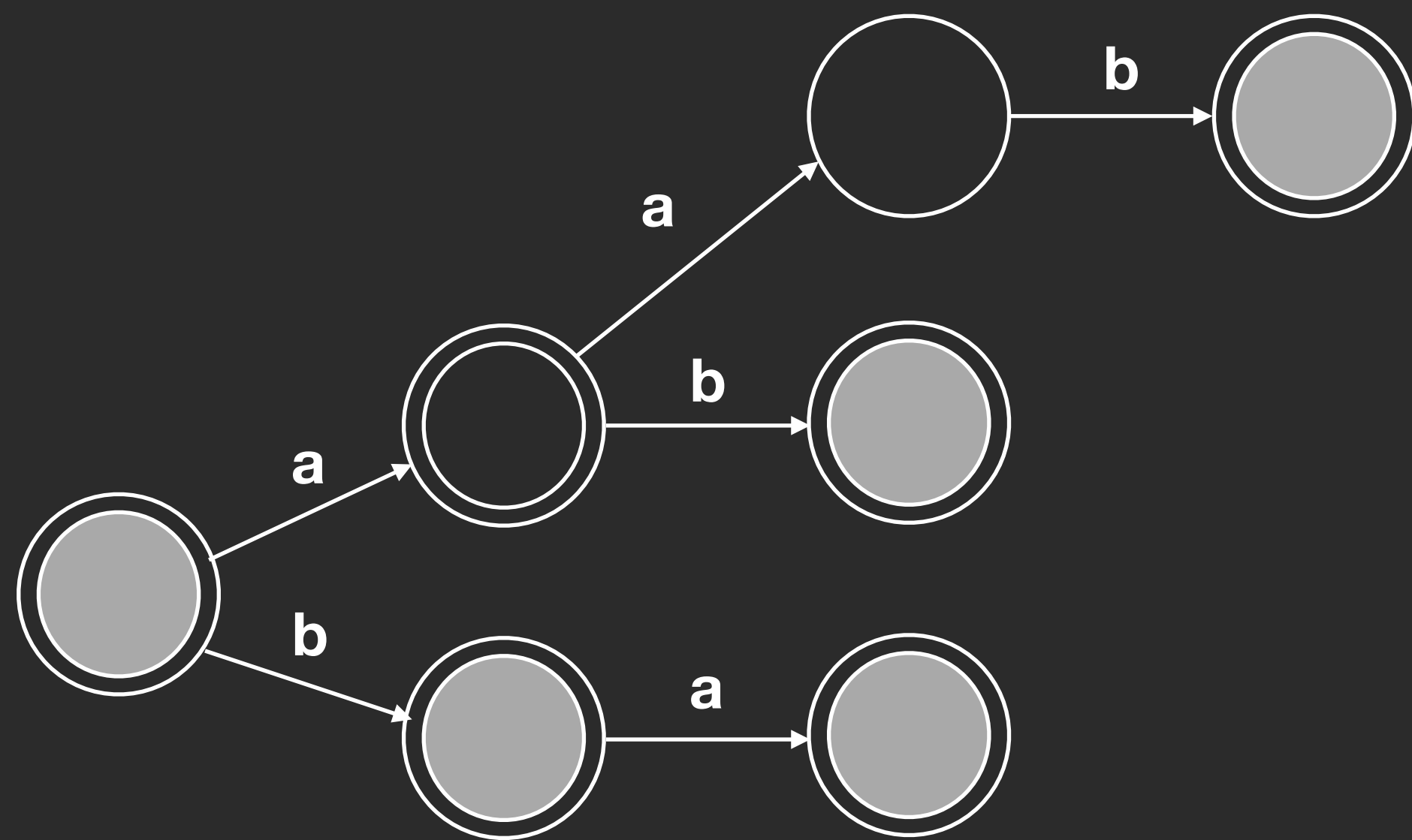


merge



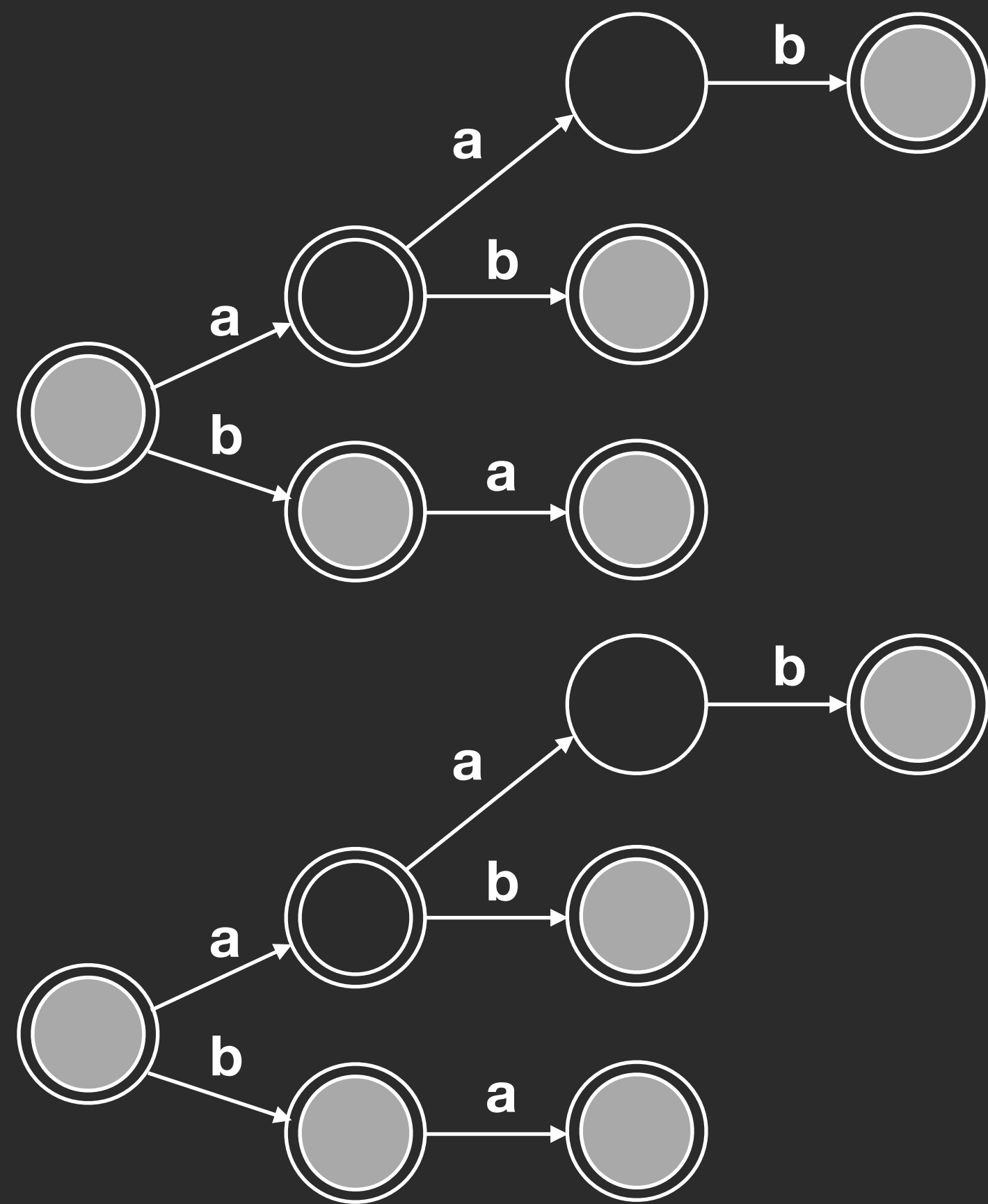
Positive: {a}    Negative: { $\emptyset$ , b, ba, ab, aab}

# State merging for decompositions



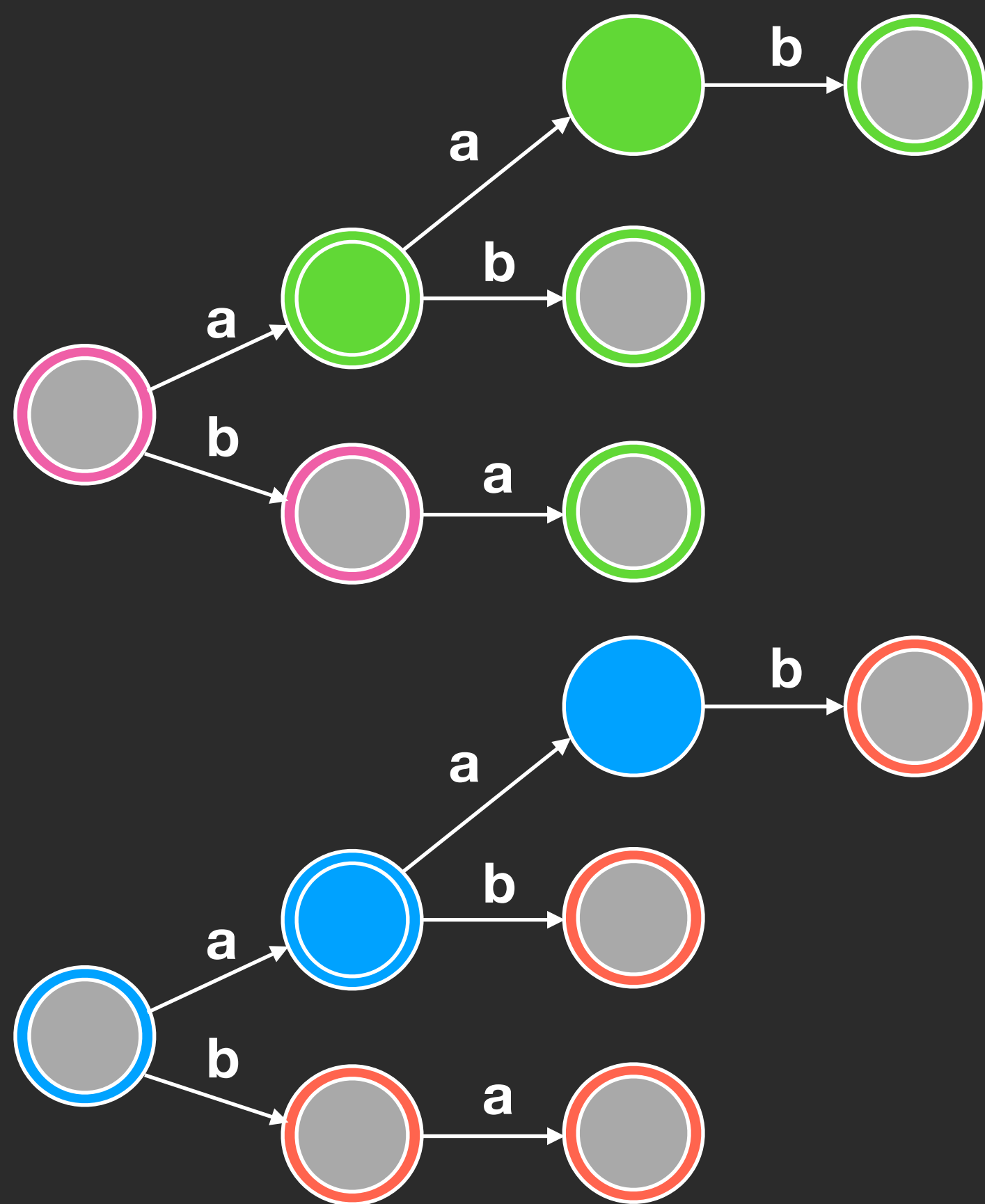
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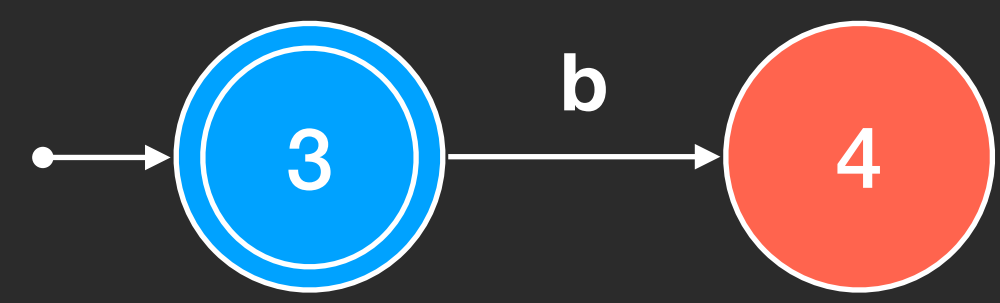
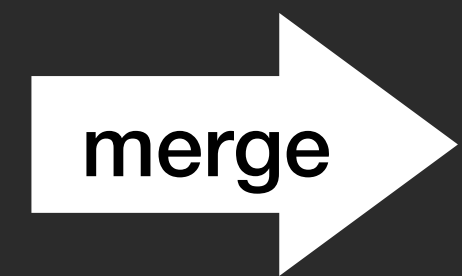
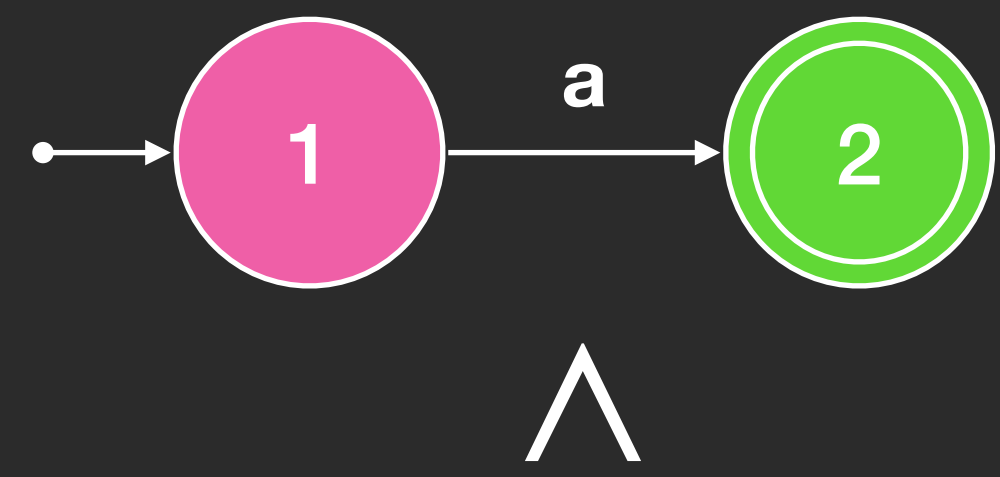
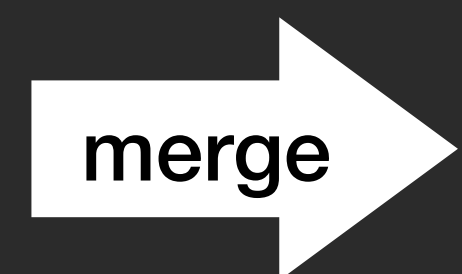
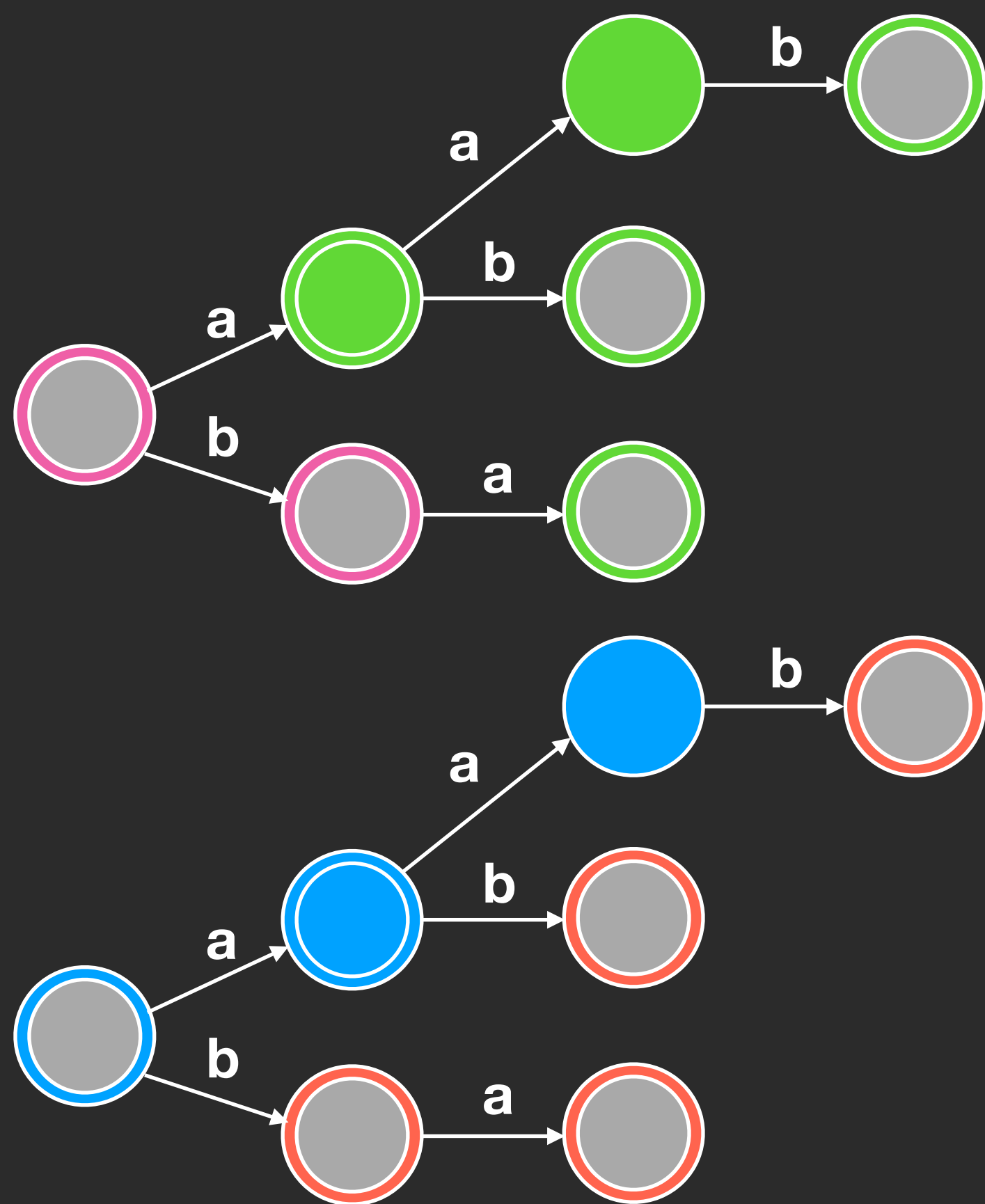
Positive: {a}    Negative: { $\emptyset$ , b, ba, ab, aab}

# State merging for decompositions



Positive: {a}    Negative: { $\emptyset$ , b, ba, ab, aab}

# State merging for decompositions



$\wedge$

Positive: {a}    Negative: { $\emptyset$ , b, ba, ab, aab}

# A SAT encoding

Implemented as an extension of existing work\*

\*Ulyantsev, Vladimir & Zakirzyanov, Ilya & Shalyto, Anatoly. (2015). BFS-based Symmetry Breaking Predicates for DFA Identification

# A SAT encoding

Implemented as an extension of existing work\*

- Each negative example must be rejected by *at least* one DFA:

$$\bigwedge_{v \in V} \bigvee_{k \in [n]} \bigwedge_{i \in [m_k]} x_{v,i}^k \implies \neg z_i^k.$$

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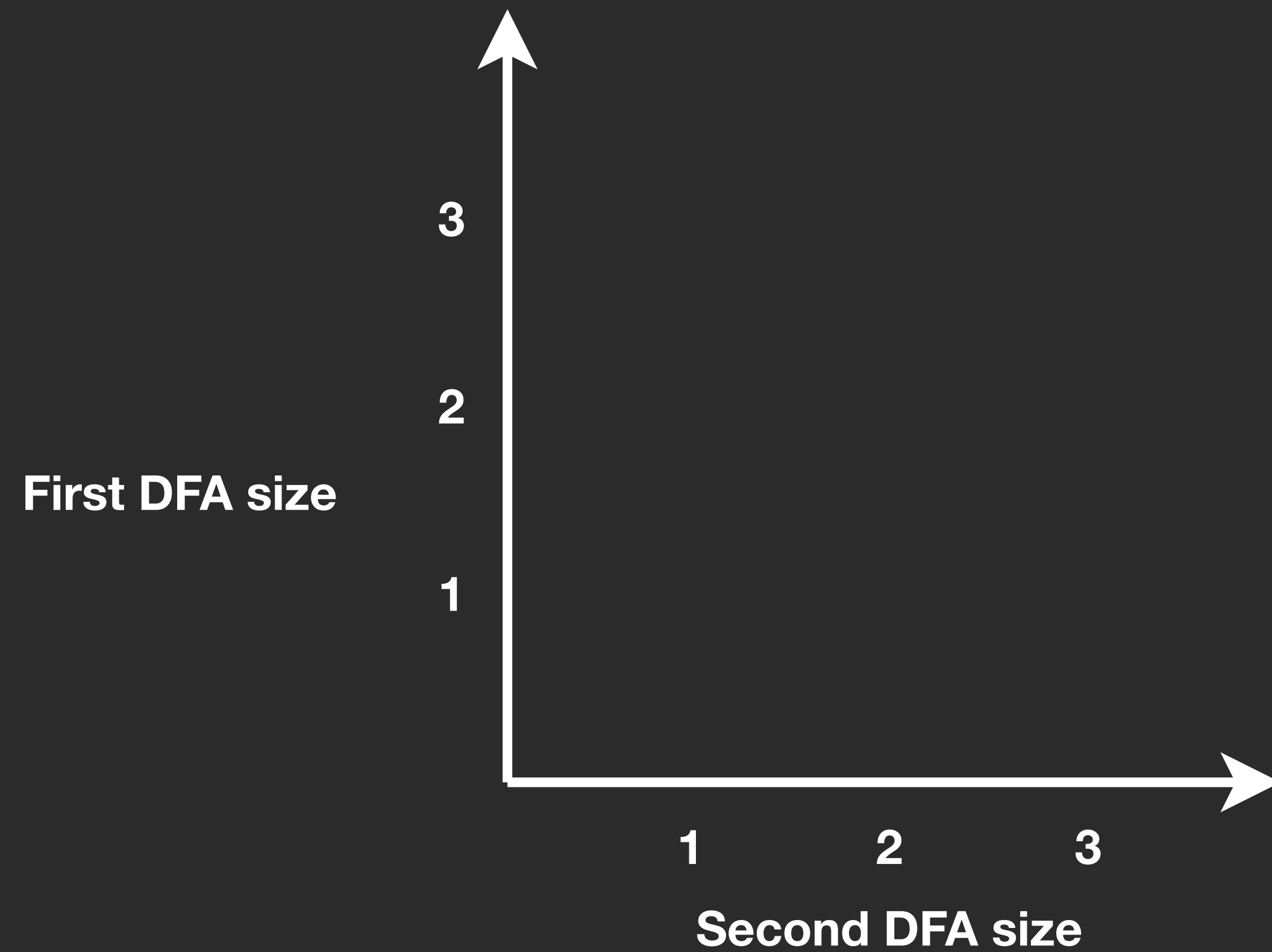
$$\bigwedge_{v \in V_-} \bigvee_{k \in [n]} \bigwedge_{i \in [m_k]} x_{v,i}^k \implies \neg z_i^k.$$

- Accepting and rejecting states of *individual* prefix trees cannot be merged:

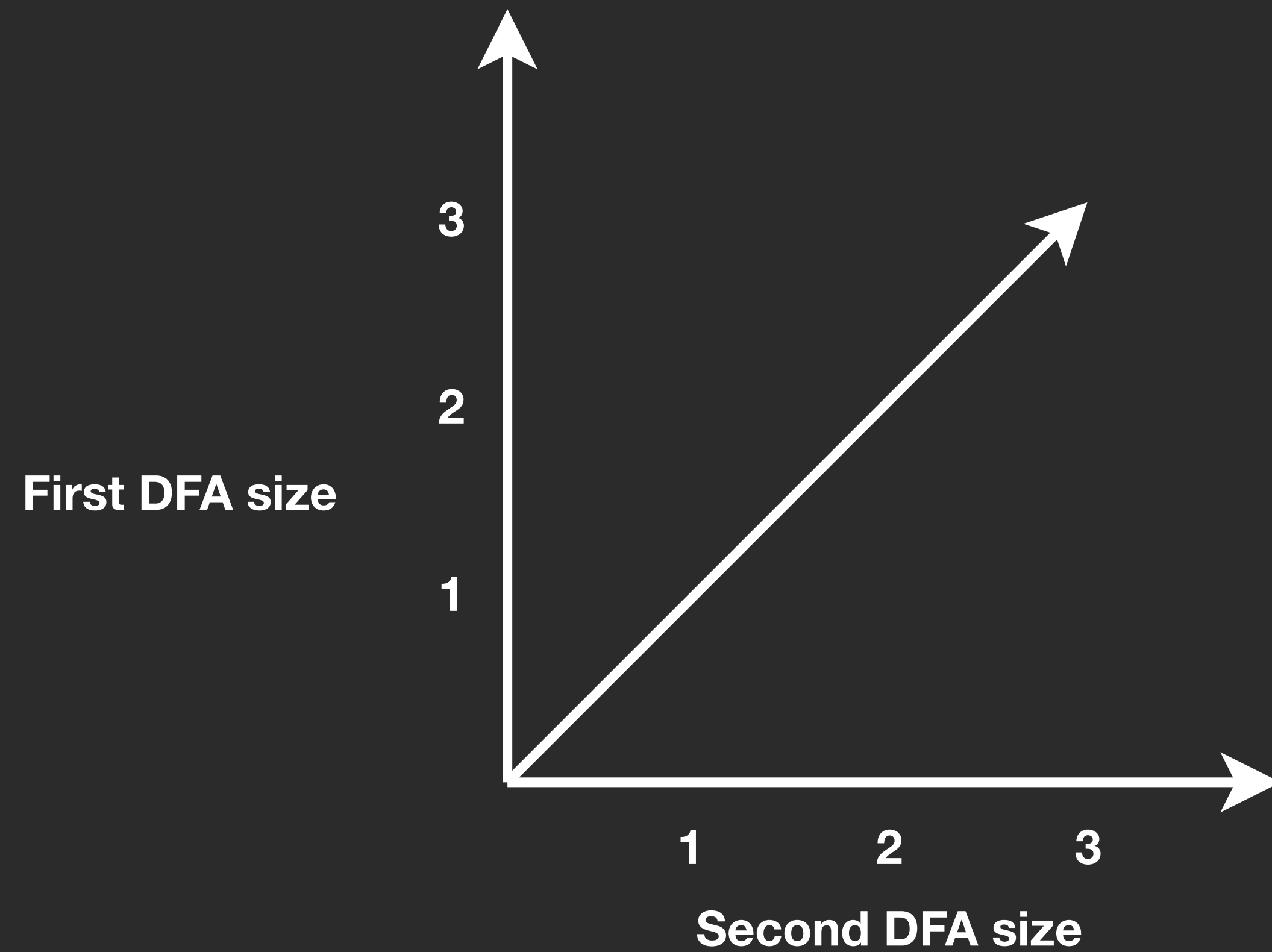
$$\bigwedge_{v_- \in V_-} \bigwedge_{v_+ \in V_+} \bigwedge_{k \in [n]} \bigwedge_{i \in [m_k]} (x_{v_-,i}^k \wedge \neg z_i^k) \implies \neg x_{v_+,i}^k$$

\*Ulyantsev, Vladimir & Zakirzyanov, Ilya & Shalyto, Anatoly. (2015). BFS-based Symmetry Breaking Predicates for DFA Identification

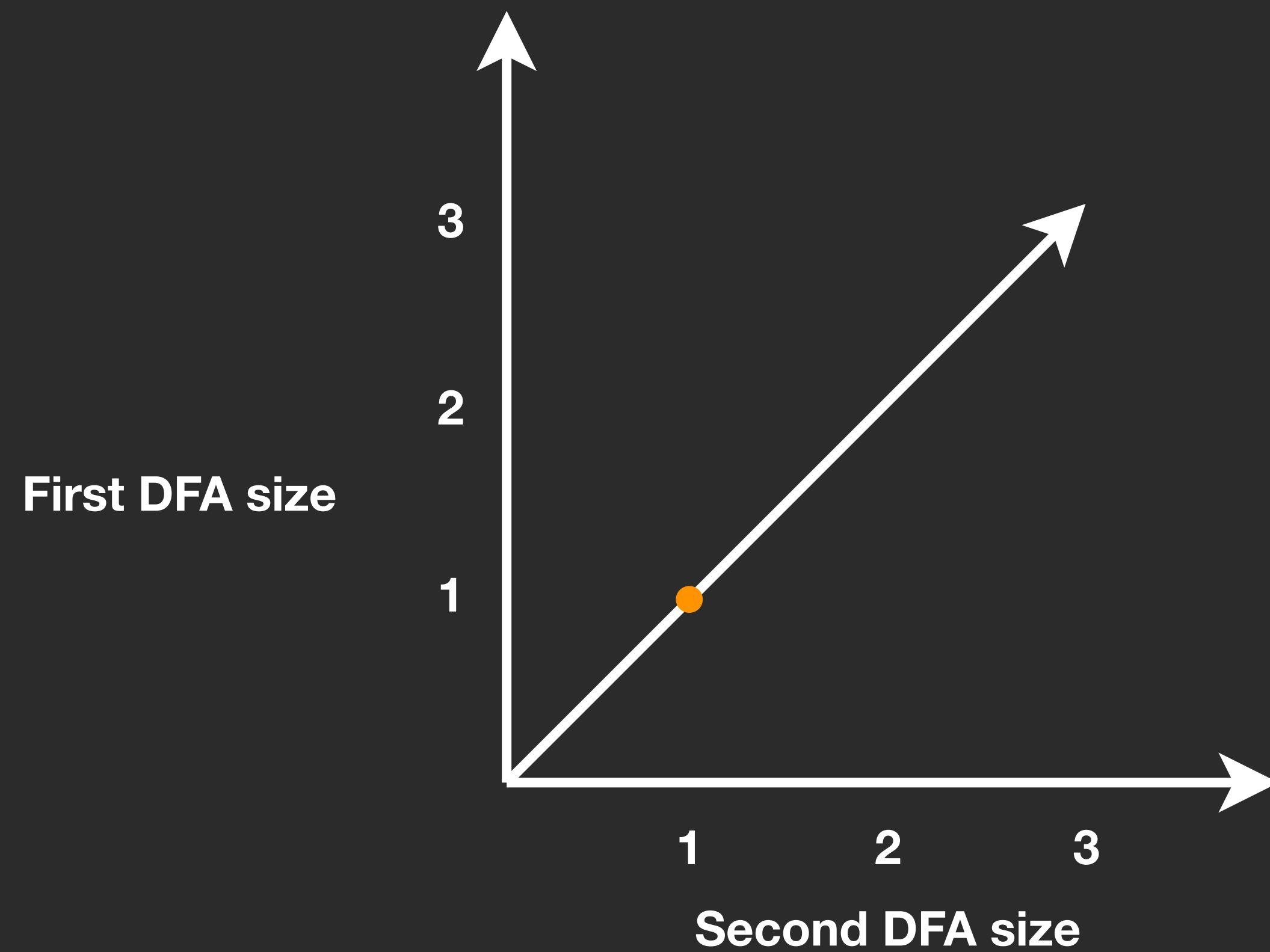
# Finding the Pareto front of minimality



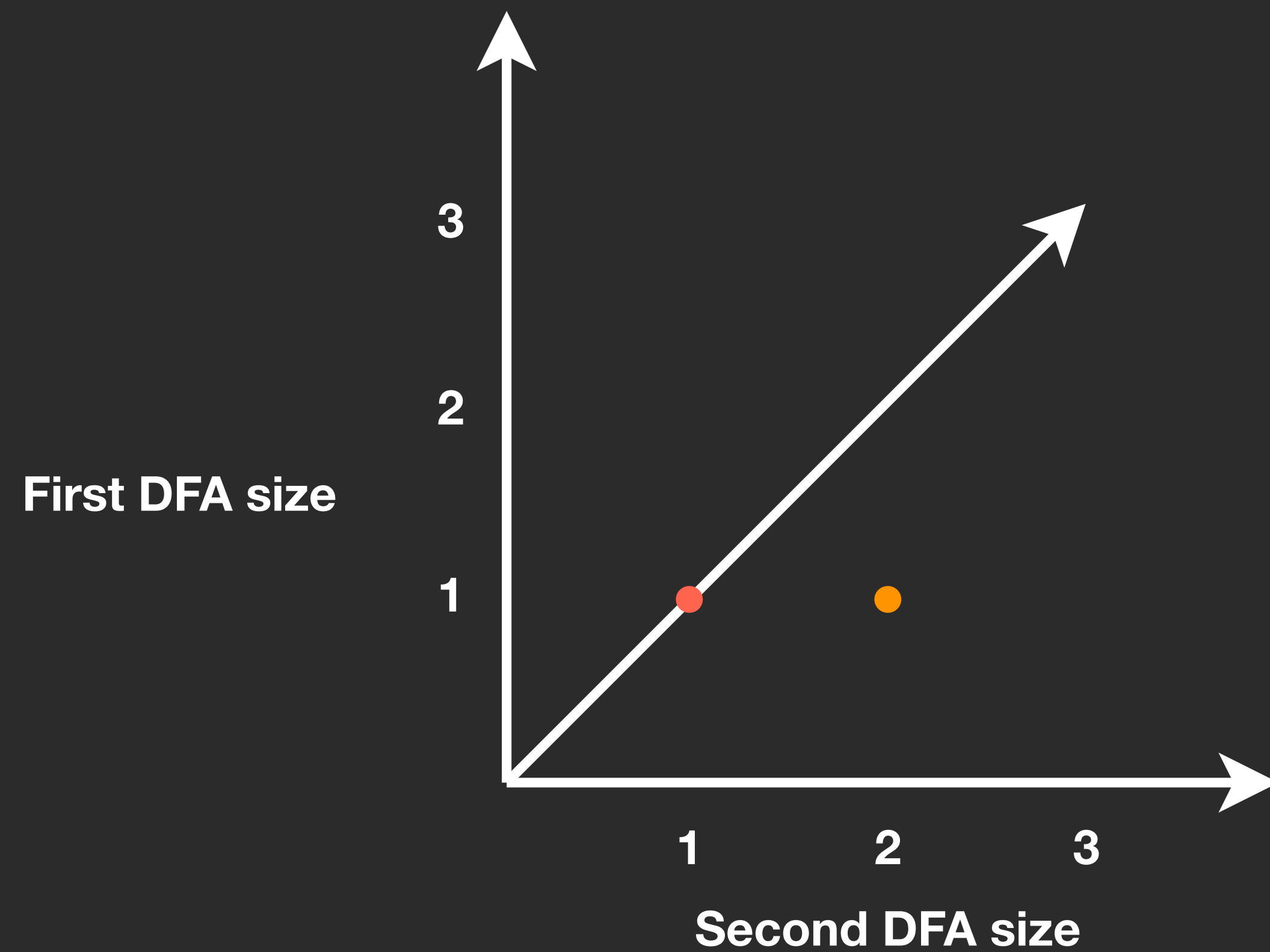
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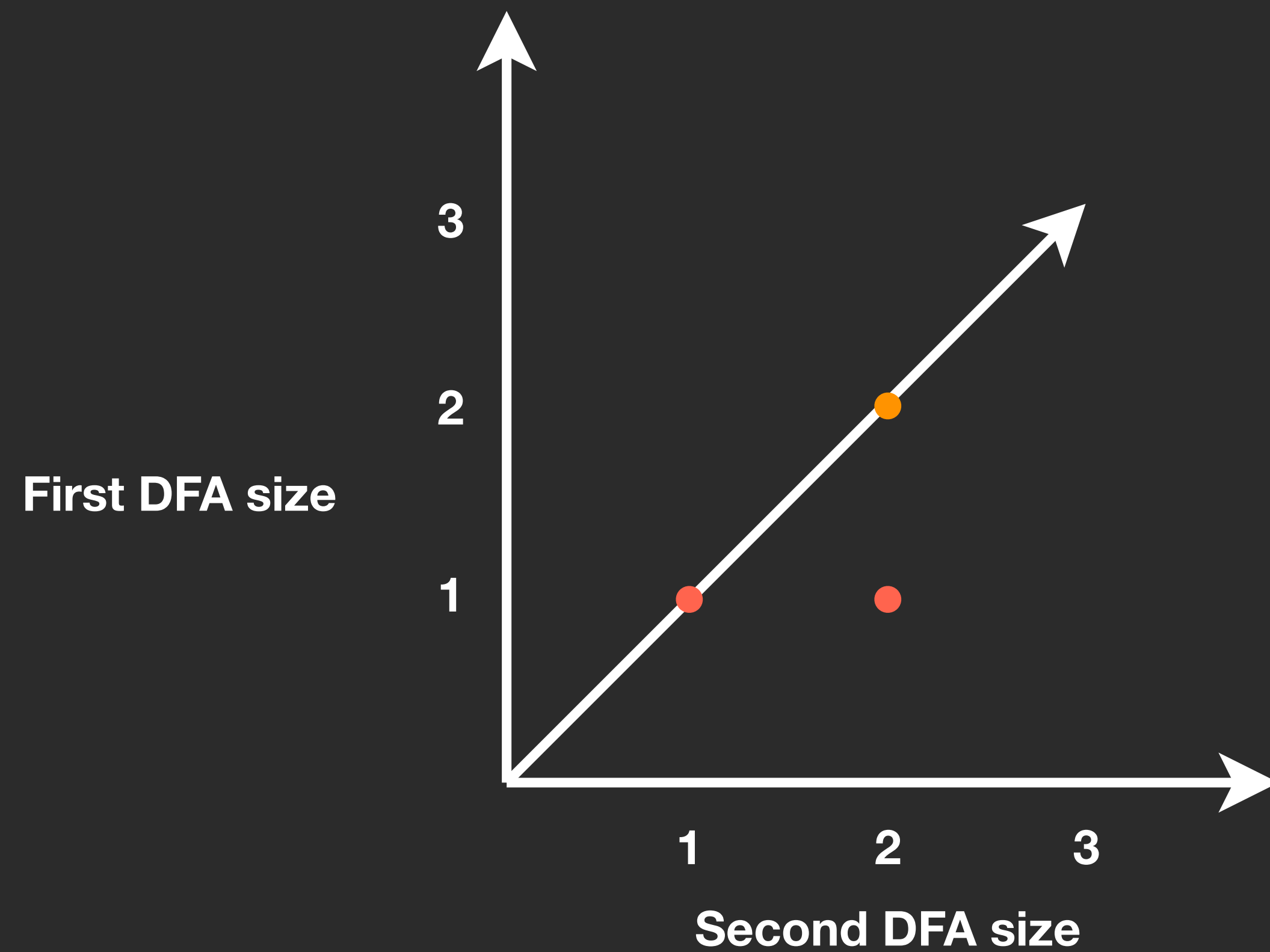
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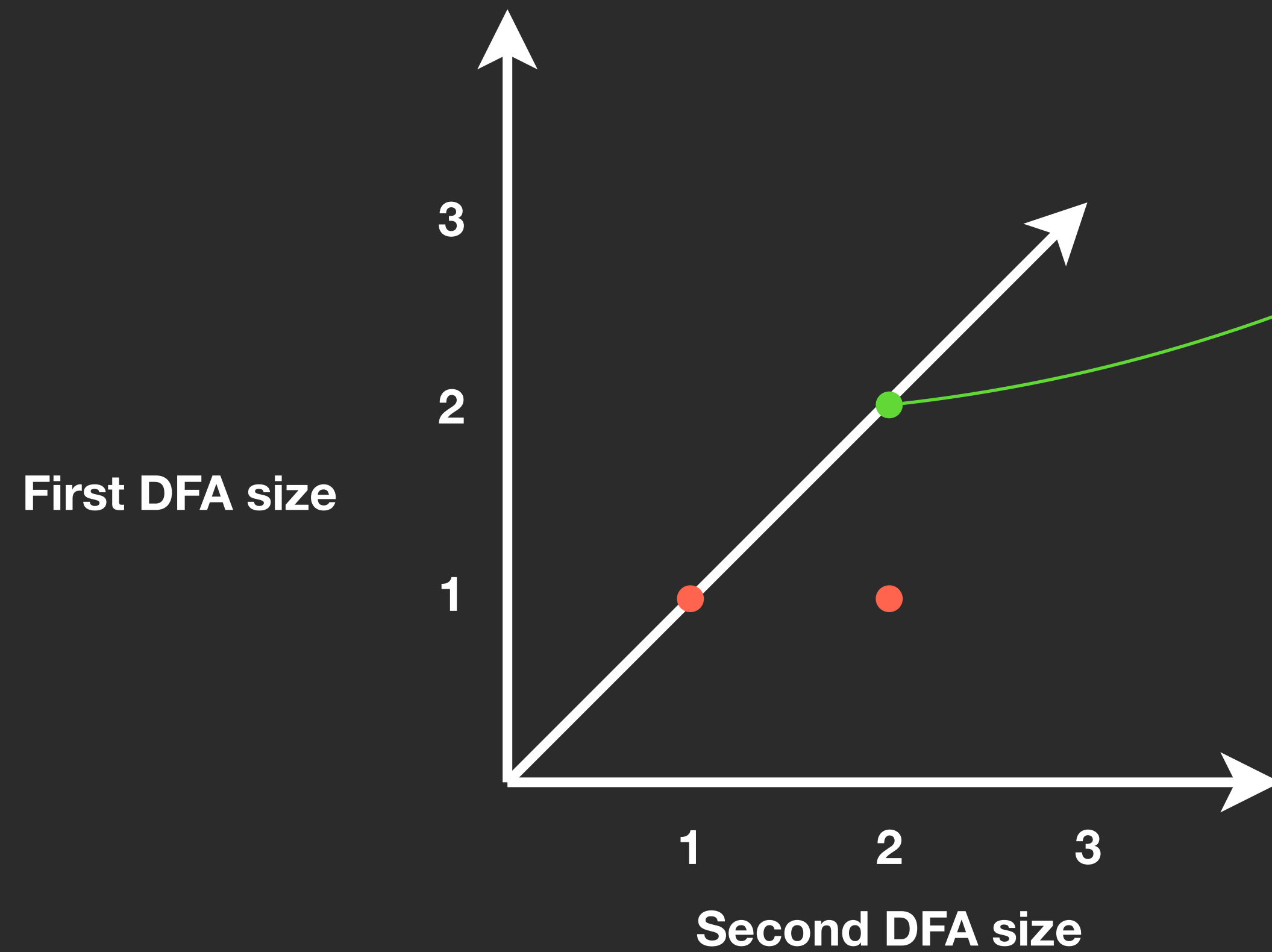
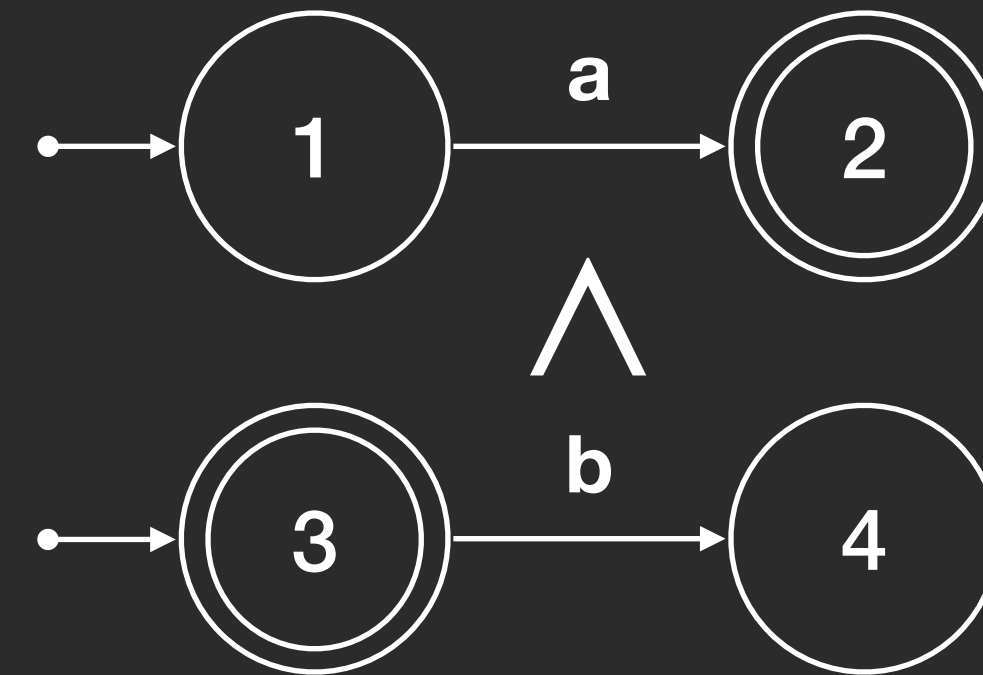
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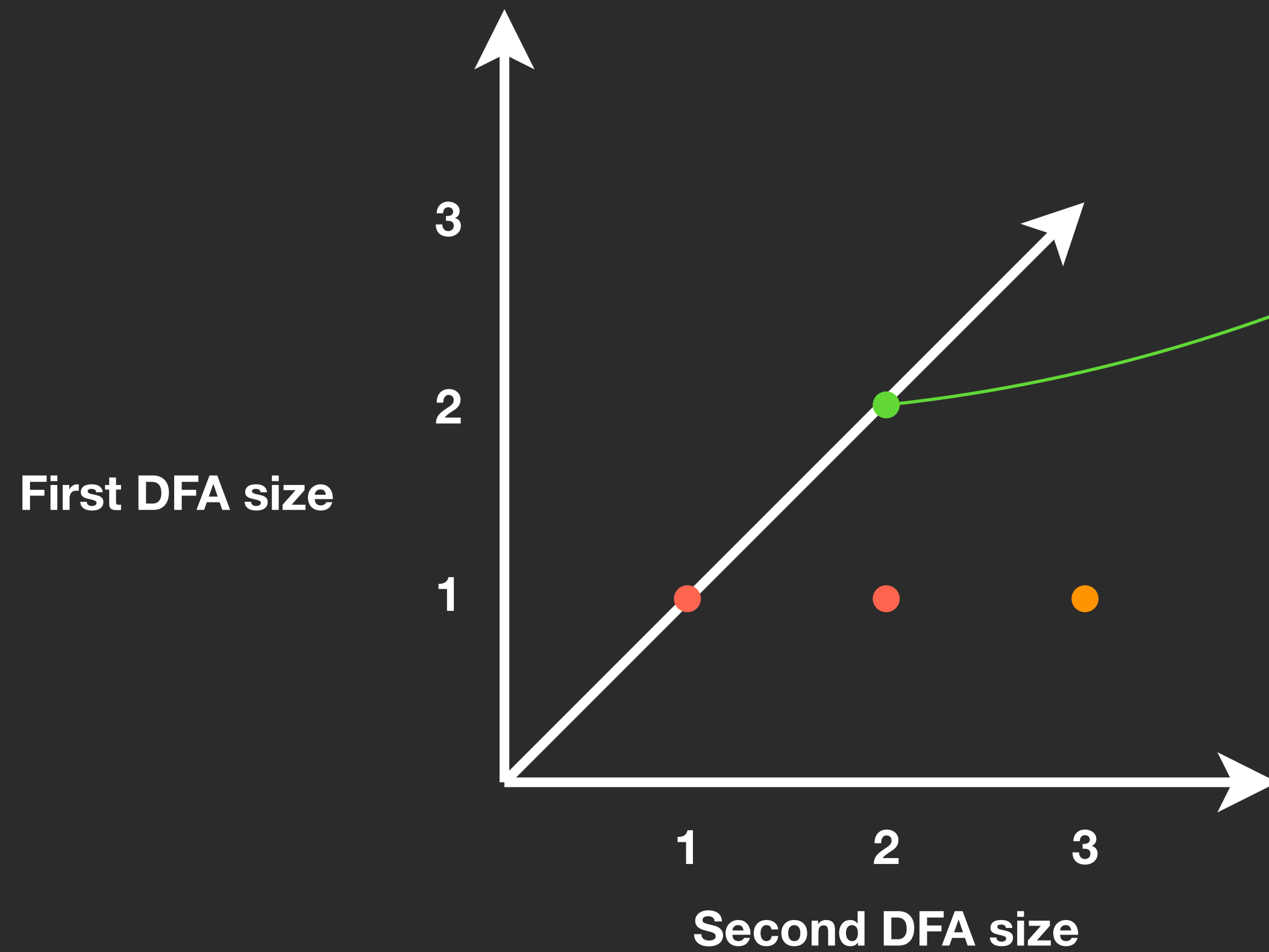
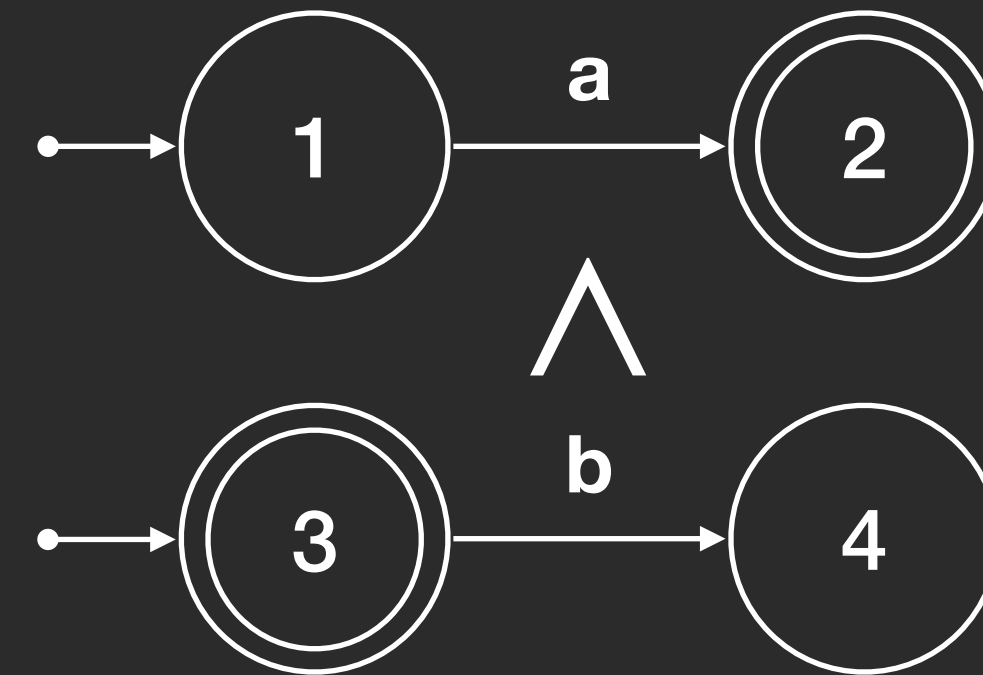
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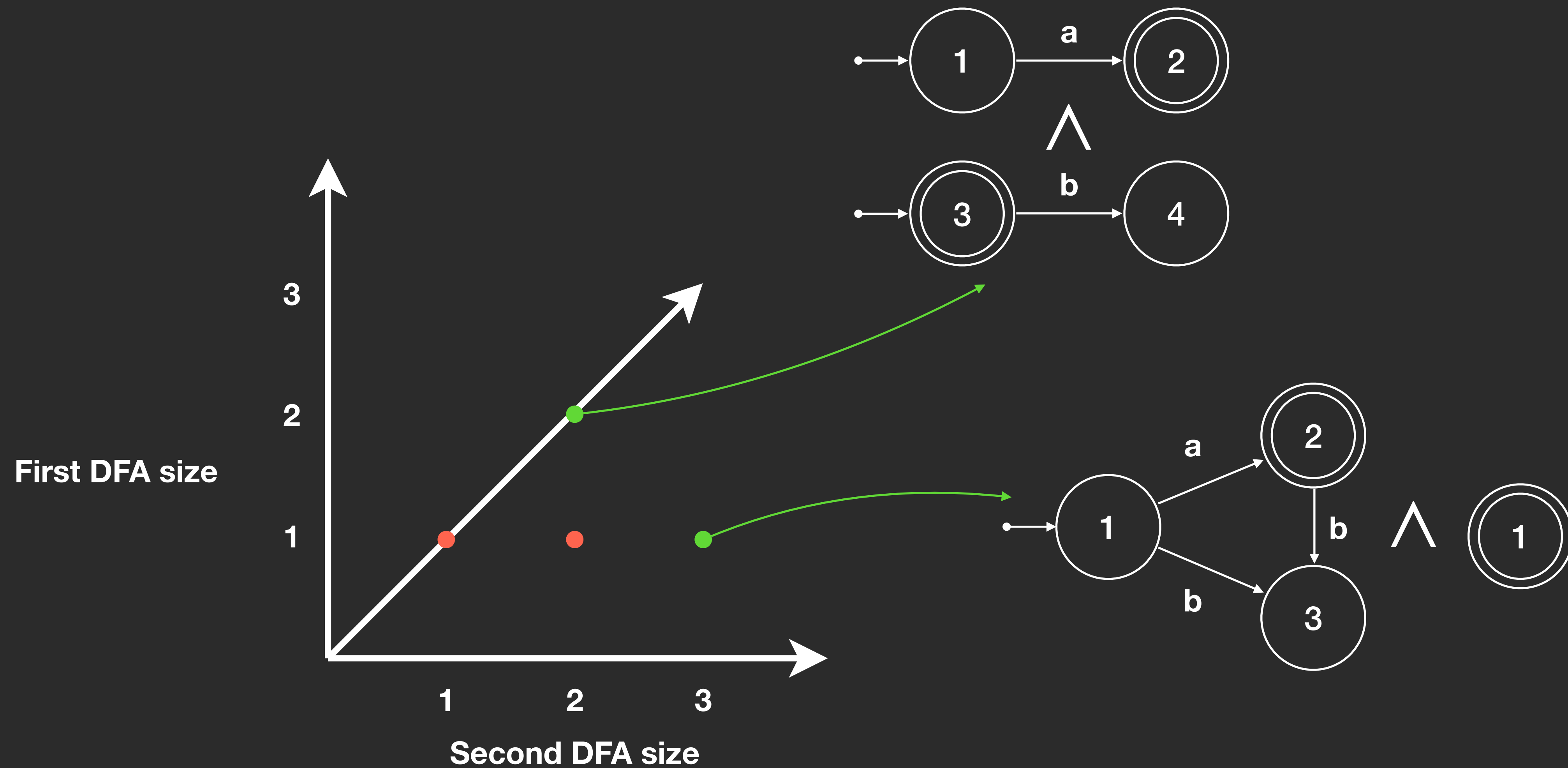


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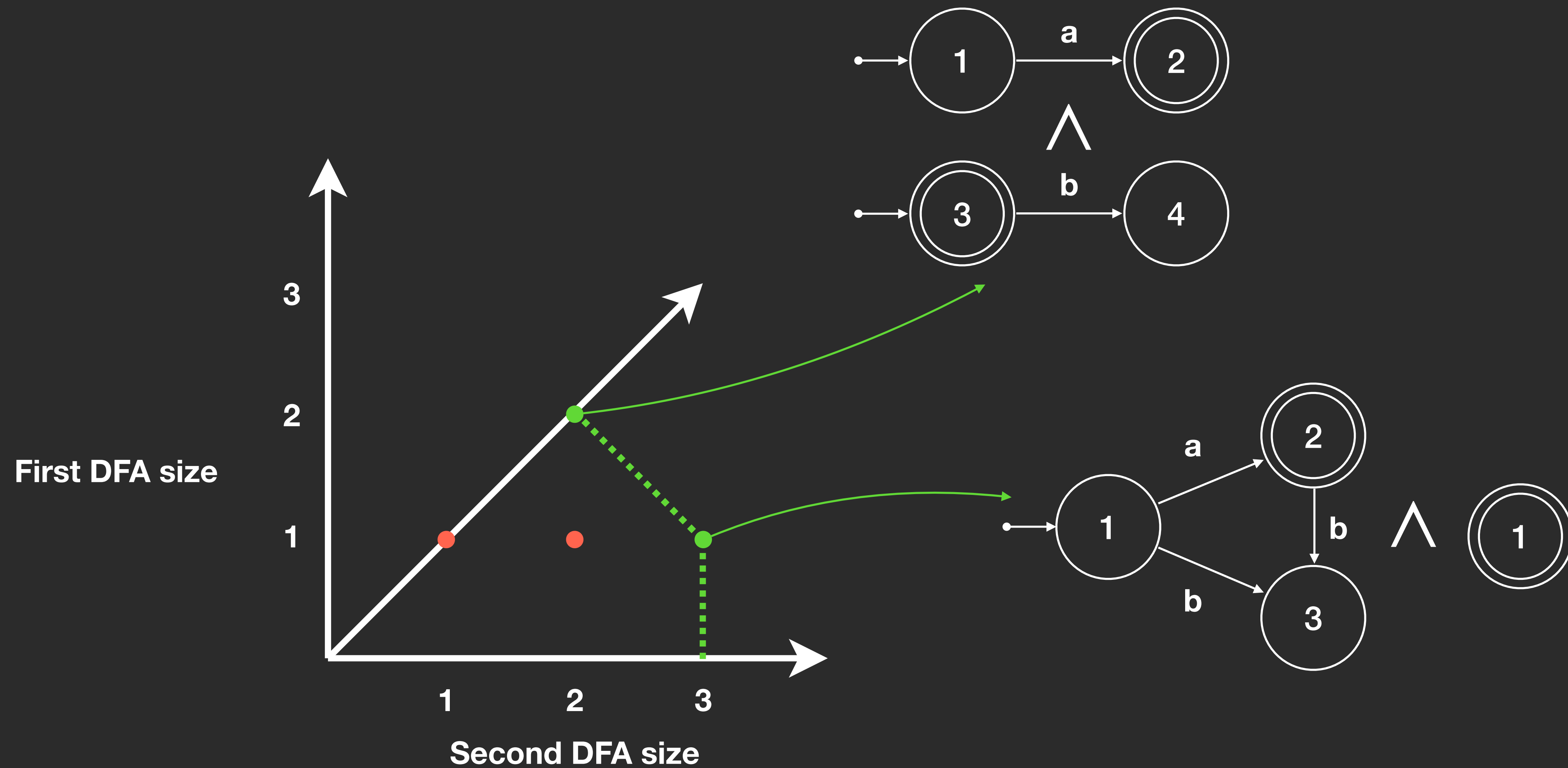




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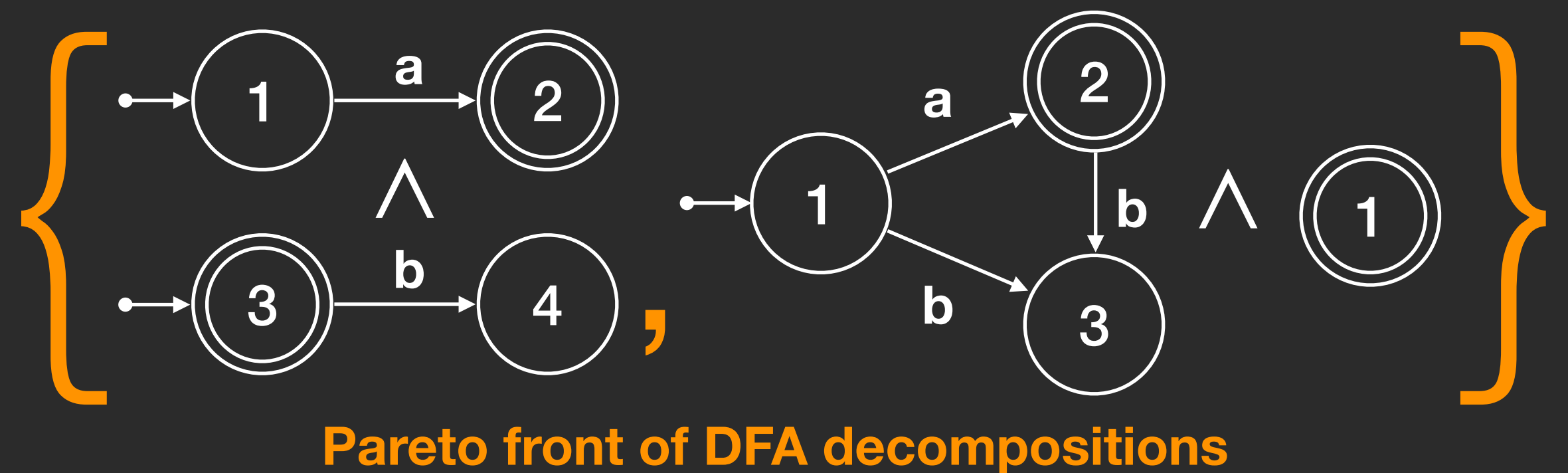


# Structure of the talk

## 1. Technical details

Examples	
Positive	Negative
a	$\emptyset$ b ba ab aab

Our algorithm



## 2. Scalability analysis

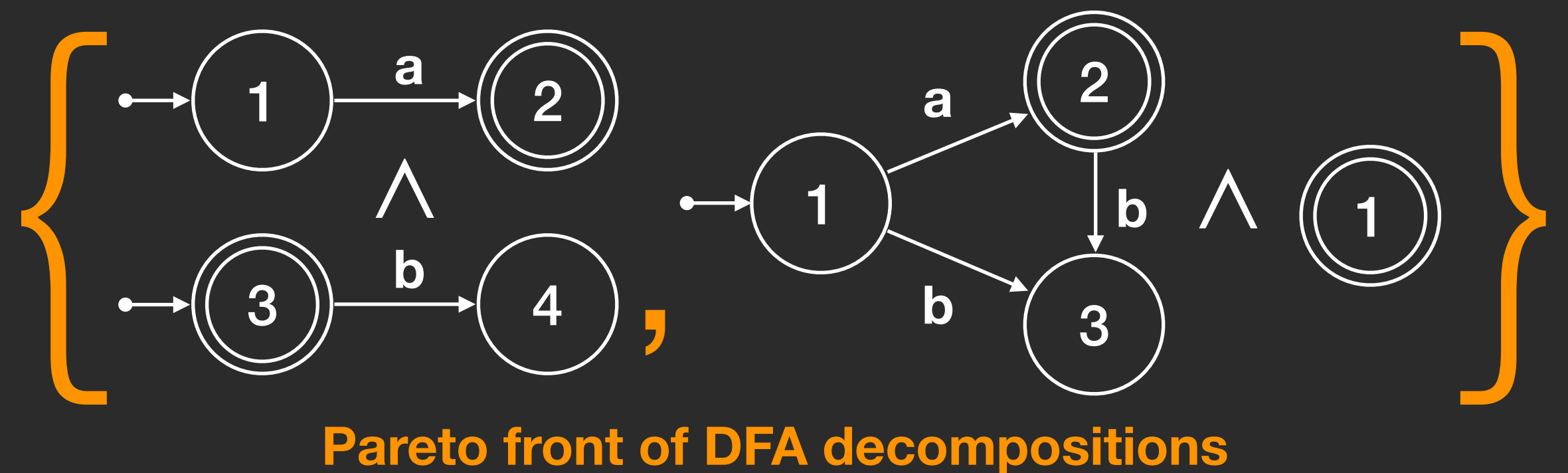
## 3. Learning from demonstrations

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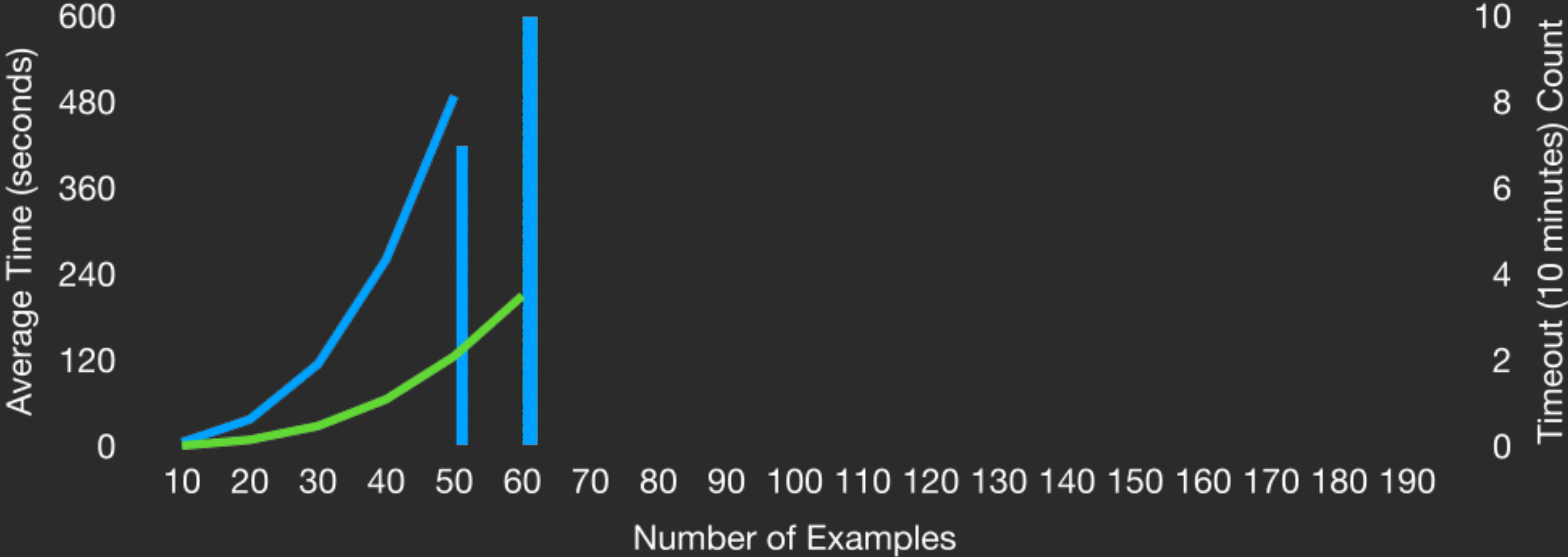
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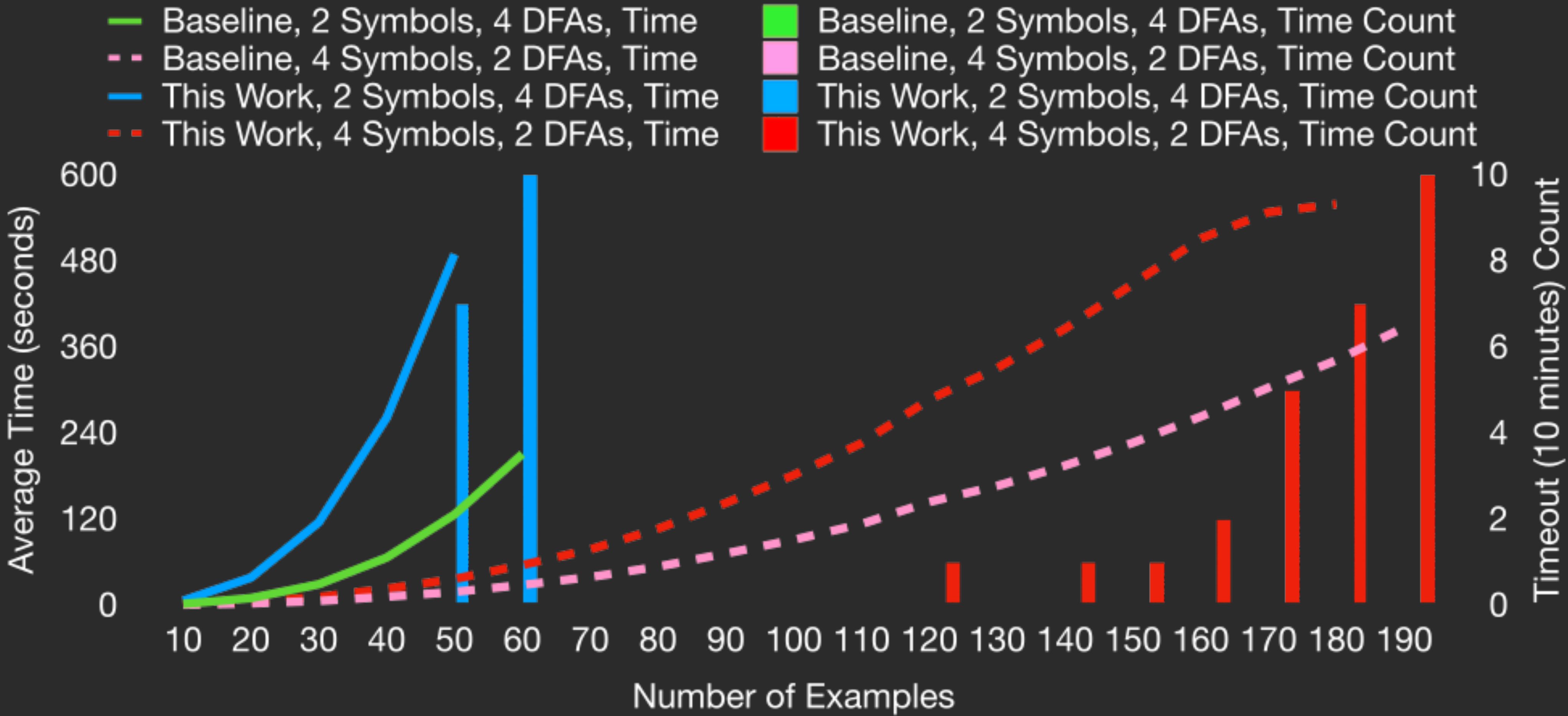
3. Learning from demonstrations

# Overhead comparable to the monolithic baseline

- Baseline, 2 Symbols, 4 DFAs, Time
- Baseline, 2 Symbols, 4 DFAs, Time Count
- This Work, 2 Symbols, 4 DFAs, Time
- This Work, 2 Symbols, 4 DFAs, Time Count



# Overhead comparable to the monolithic baseline



# Structure of the talk

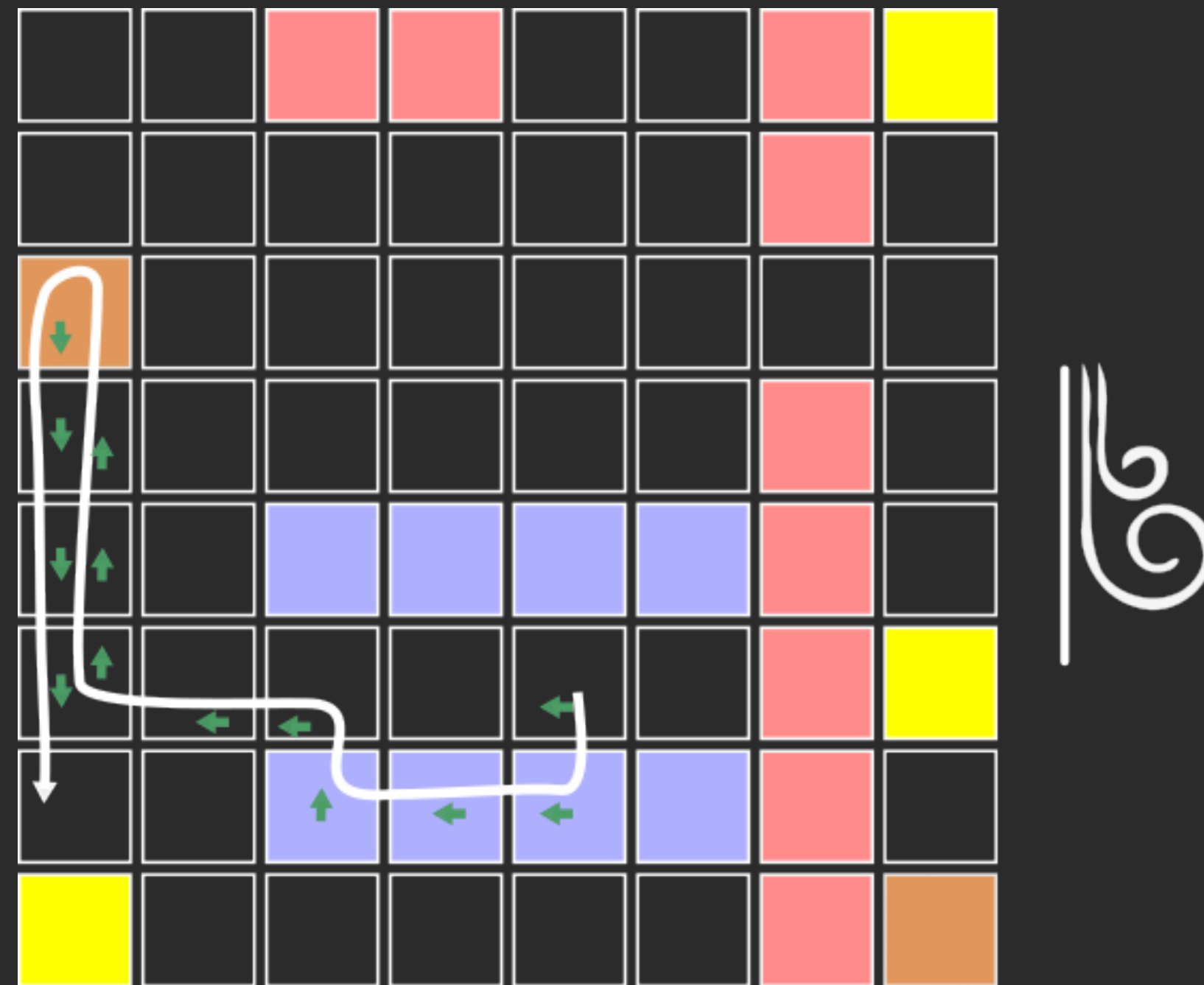
1. Technical details

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# Learning from demonstrations



Actions = { $\uparrow$   $\downarrow$   $\leftarrow$   $\rightarrow$ }

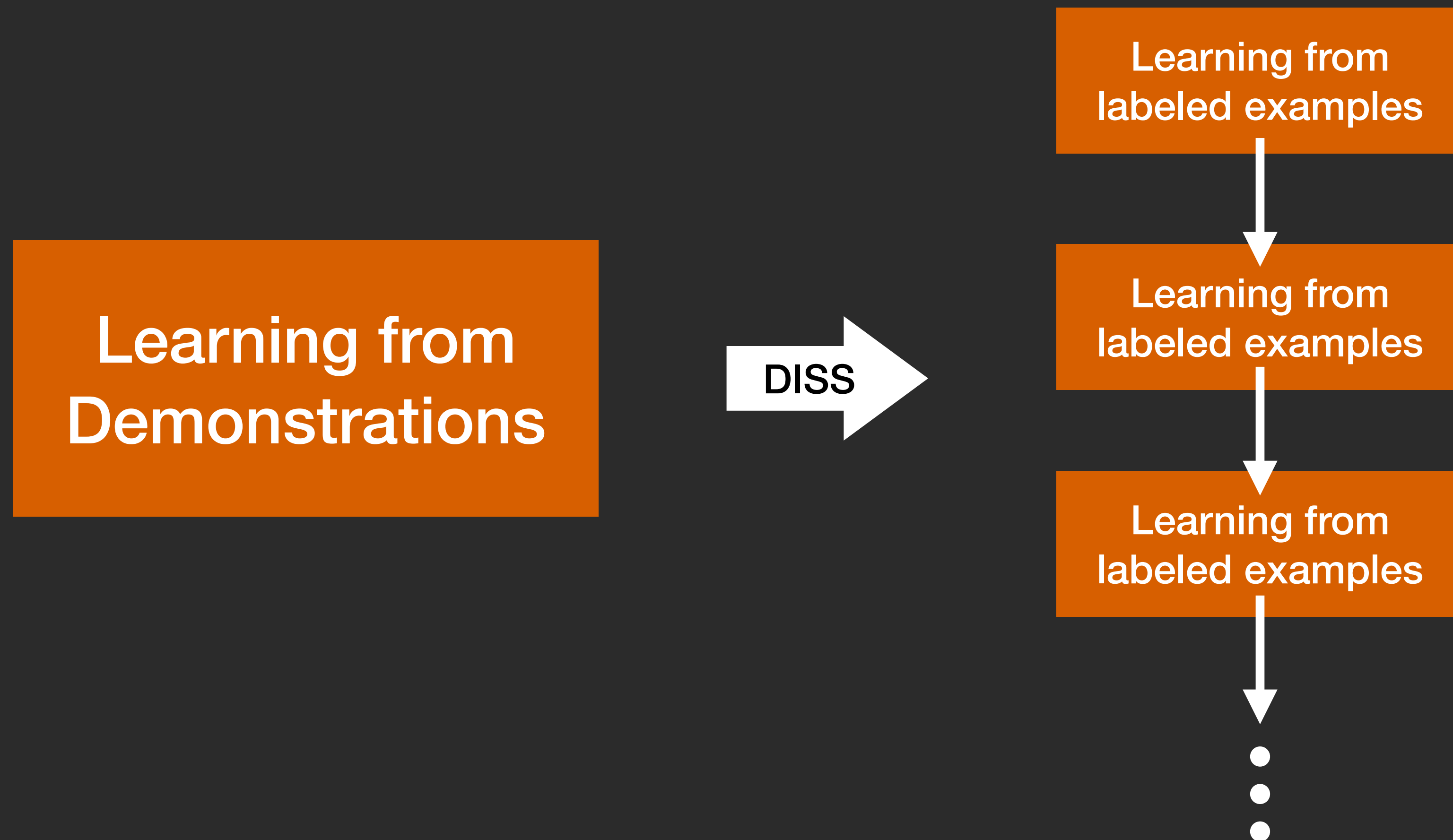
$\Pr(\text{slip } \downarrow) = 1/32$

# Demonstration Informed Specification Search (DISS)

Learning from  
Demonstrations

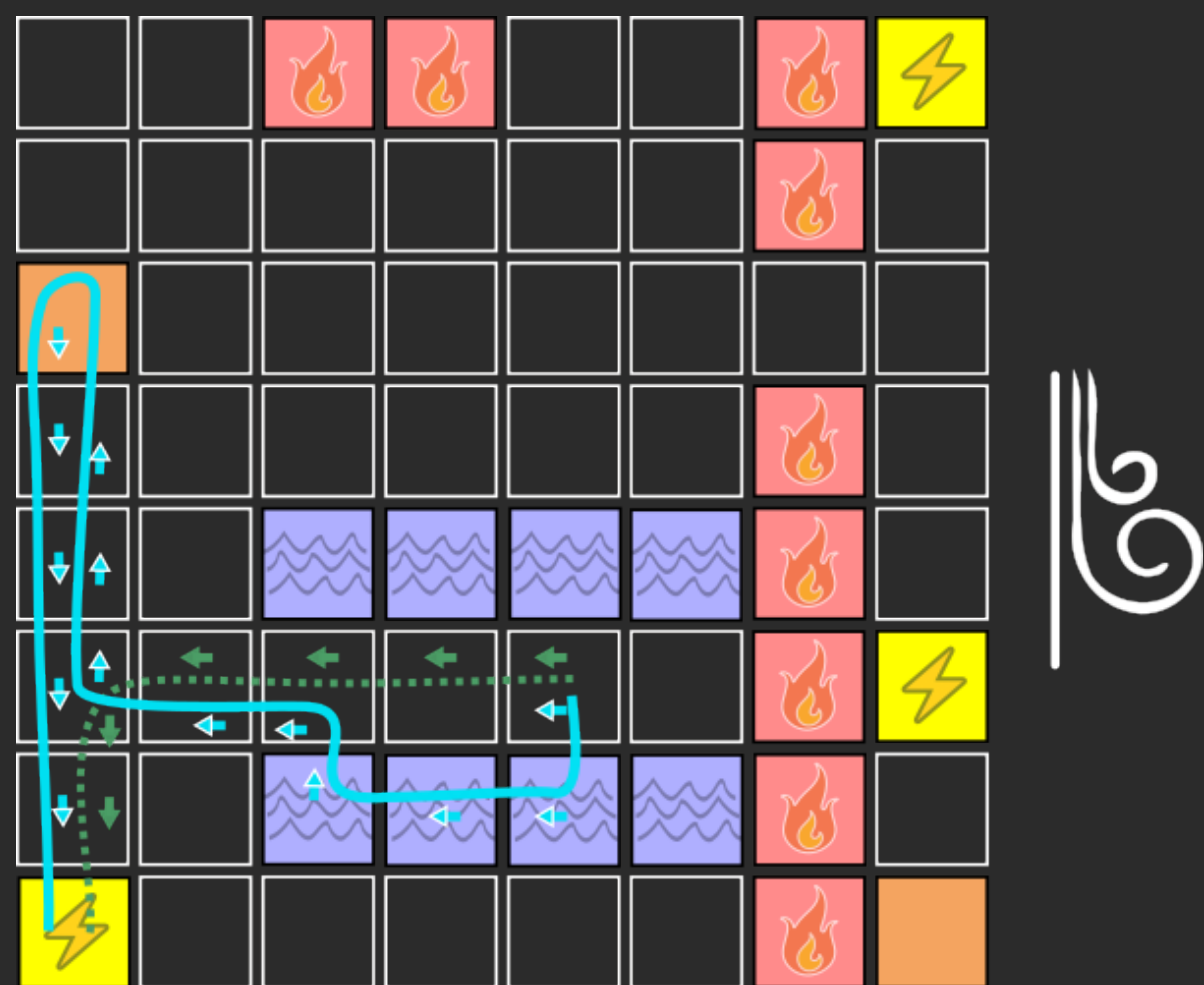
\*Vazquez-Chanlatte, Marcell Jose. Specifications from Demonstrations: Learning, Teaching, and Control. Diss. UC Berkeley, 2022.

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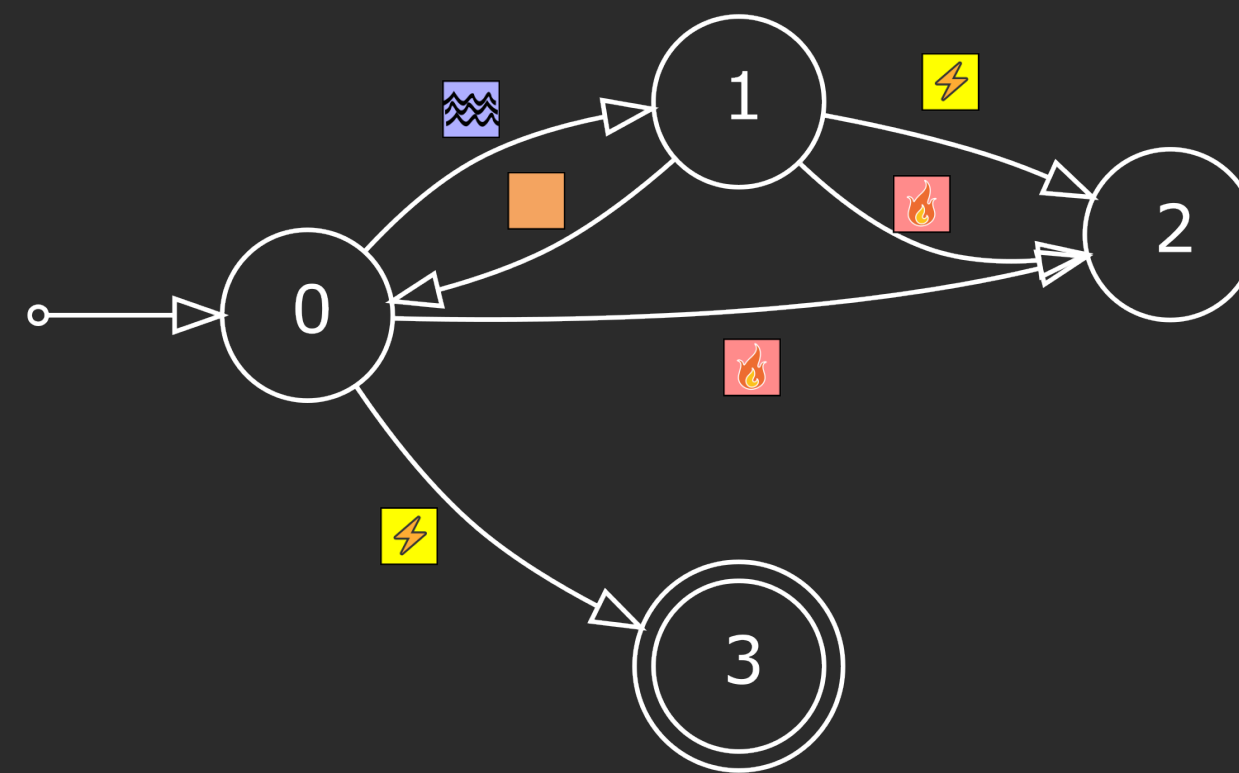
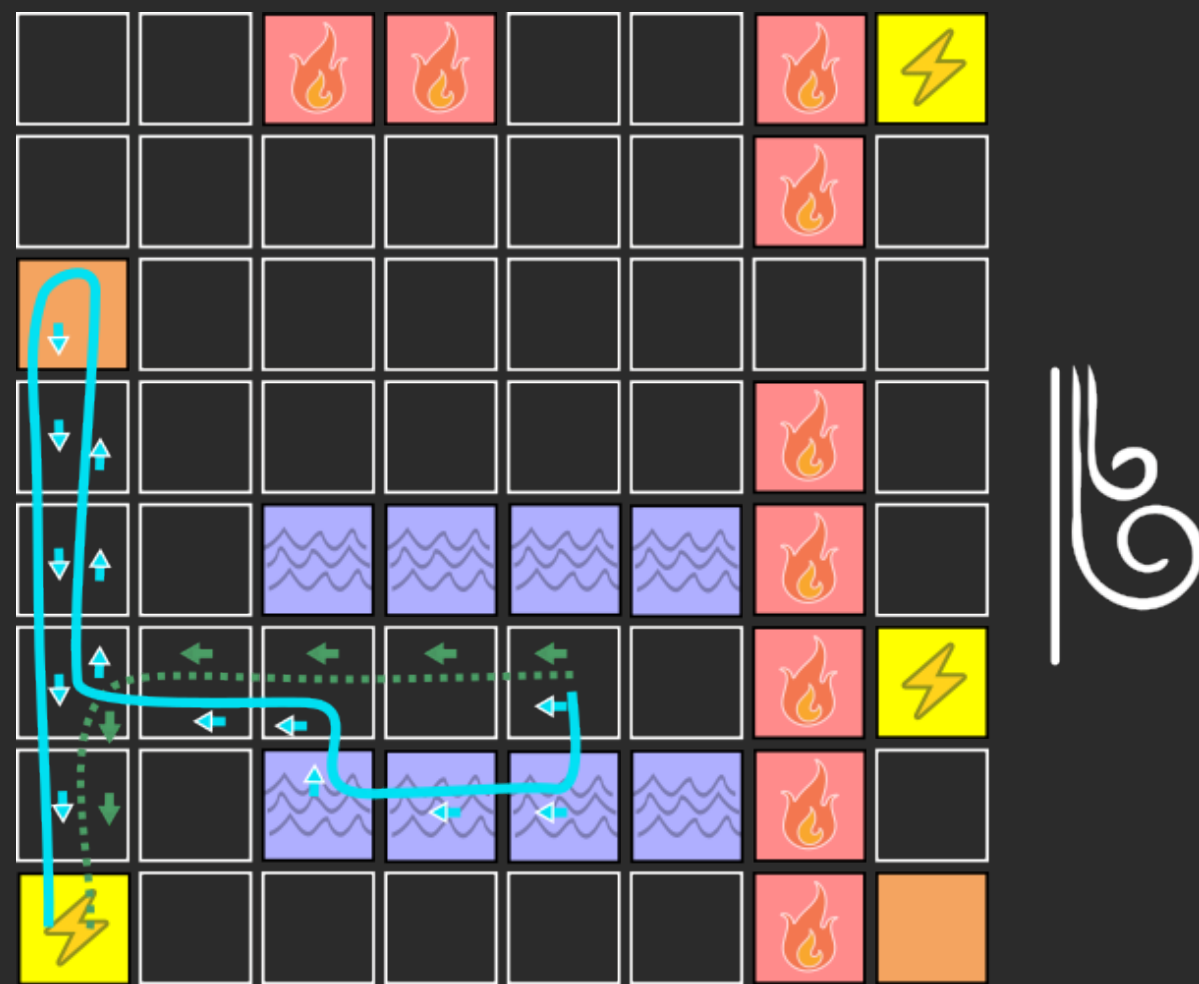
\*Vazquez-Chanlatte, Marcell Jose. Specifications from Demonstrations: Learning, Teaching, and Control. Diss. UC Berkeley, 2022.

# A helpful inductive bias from decompositions



Reach ⚡ while avoiding 🔥. If you ever touch 🌊, you must then touch 🟠 before reaching ⚡.

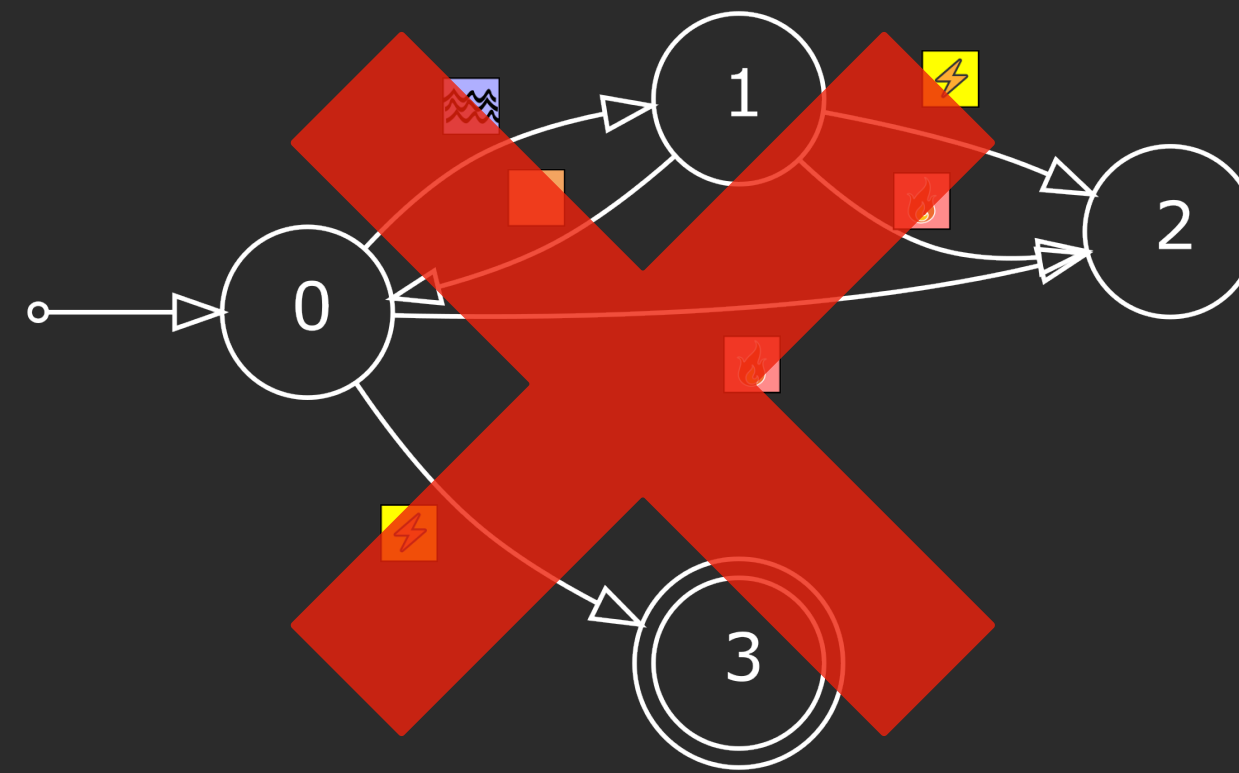
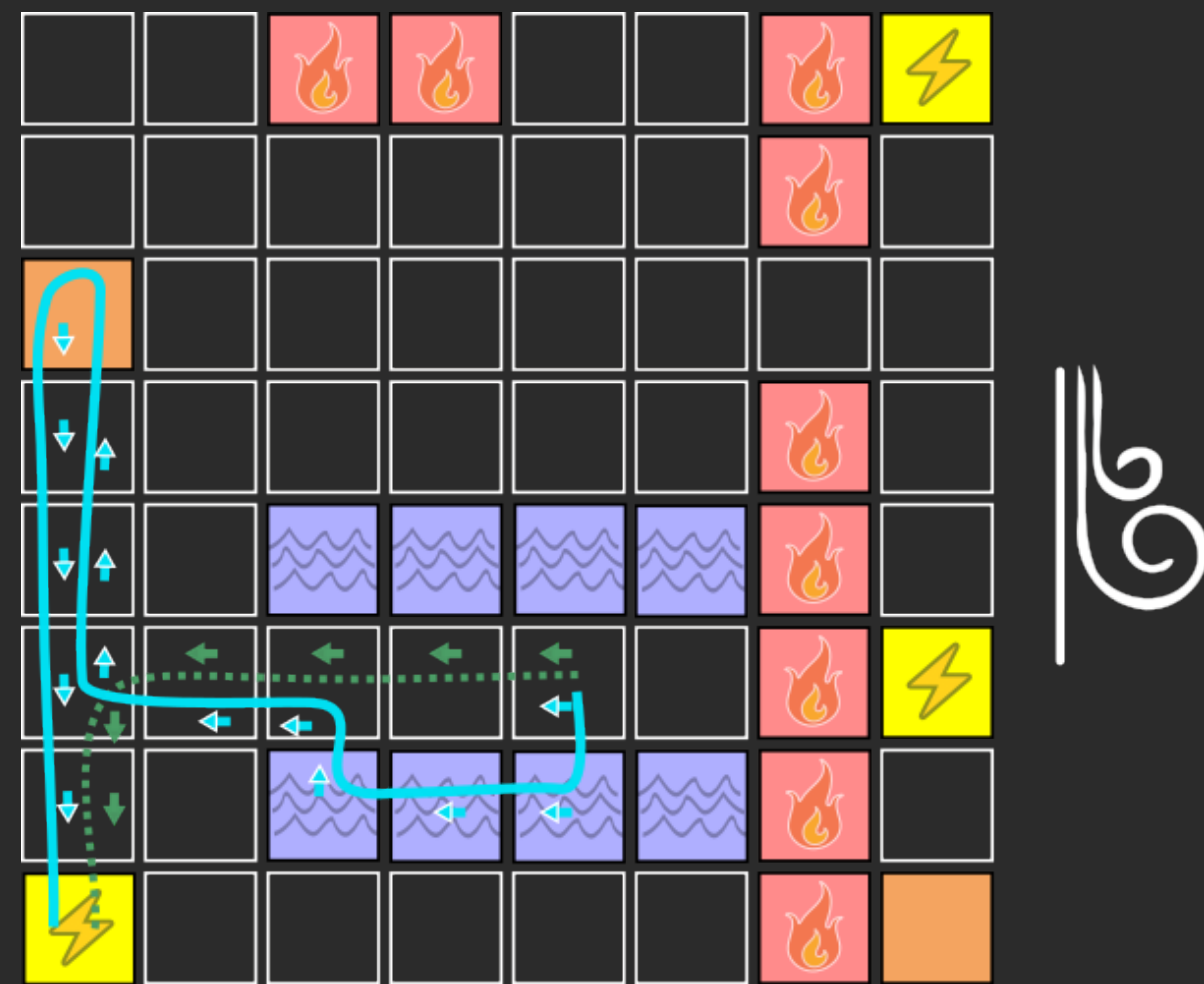
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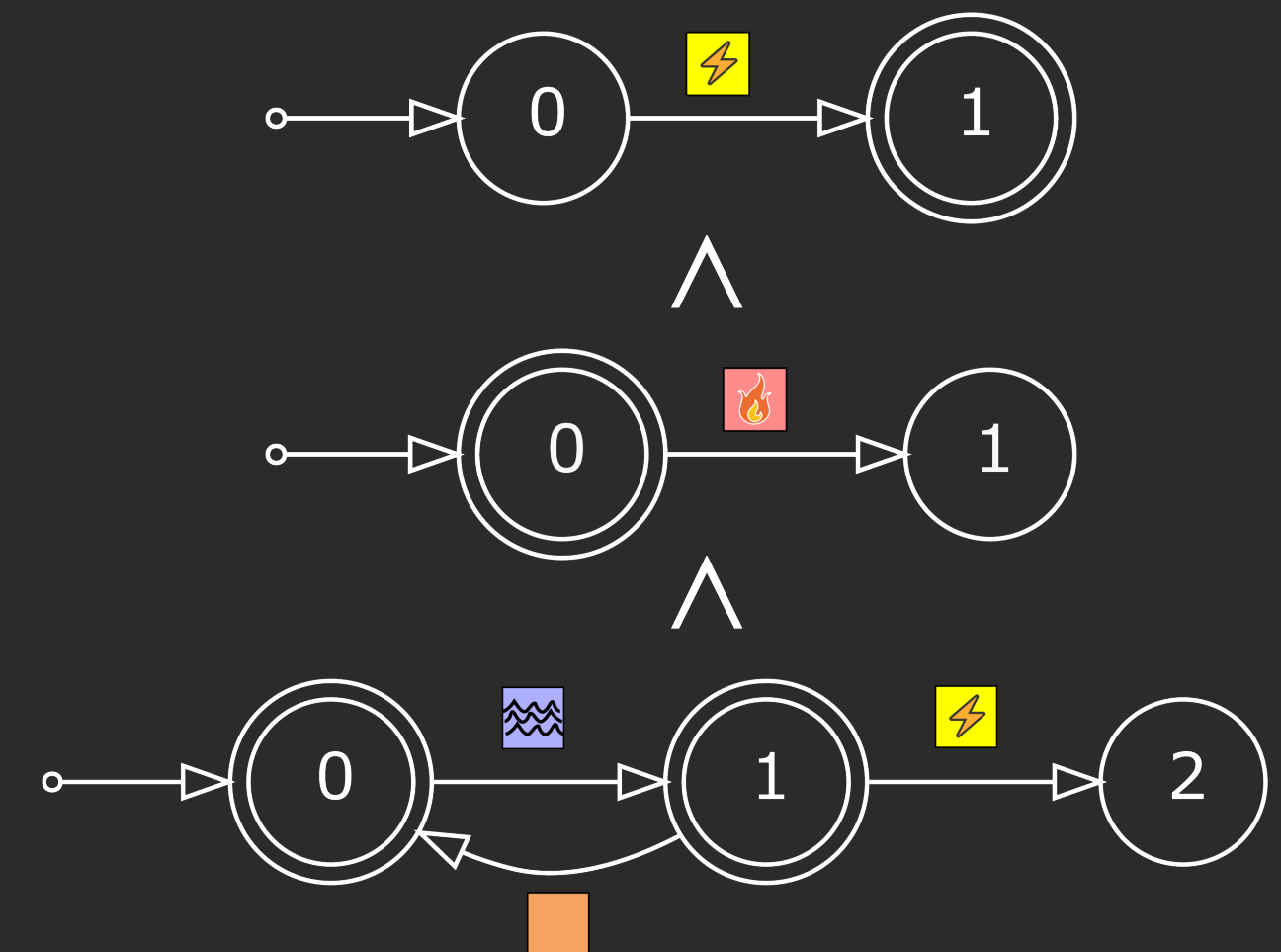
Identified monolithic DFA  
(incorrect)

Reach ⚡ while avoiding 🔥. If you ever touch 💧, you must then touch 🧱 before reaching ⚡.

# A helpful inductive bias from decompositions



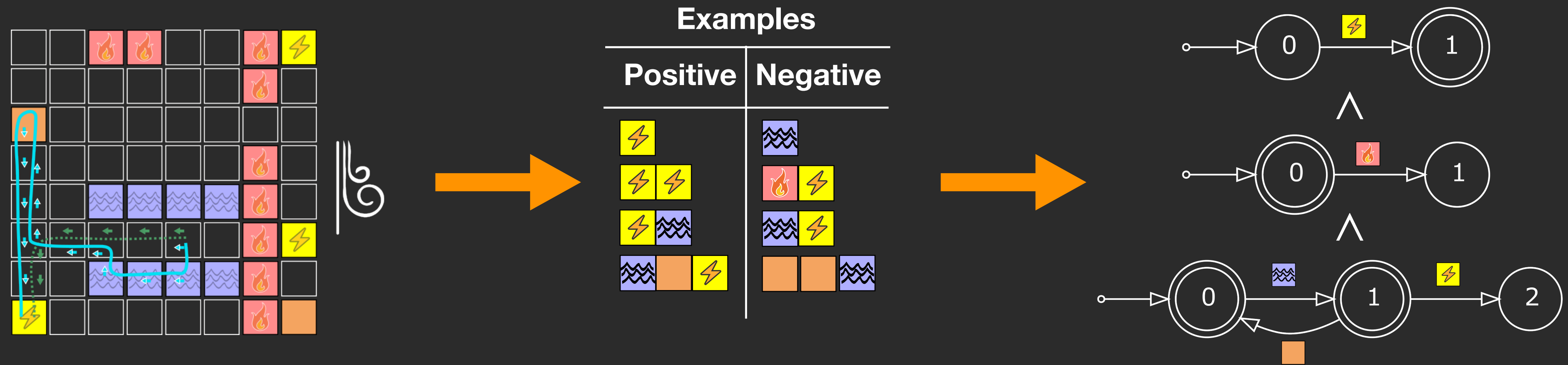
Identified monolithic DFA  
(incorrect)



Identified DFA decomposition  
(correct)

Reach ⚡ while avoiding 🔥. If you ever touch 🌊, you must then touch 🟠 before reaching ⚡.

# Conclusion



- Known symmetry-breaking optimization still missing from the encoding
- Easy to extend to disjunctions and boolean combinations of DFAs